Symbolic Machine Learning for Interpretable Al Recent advancements and future directions

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Human-Like Learning

"Human thought can be seen as a model-building activity. Human-like learning is the process of such model-building" [1]

Humans are capable of performing cognitive activities:

- Learning from past experience
 (e.g., building models of the world that can explain the observations).
- Making predictions and generating explanations
 (e.g., use learned models to generate understanding and explanation of observations)
- Revising and extending learned knowledge, based on new information (e.g., enable compositionality of learned models)
- Communicate their learned knowledge to others (e.g., support interpretability of learned models)

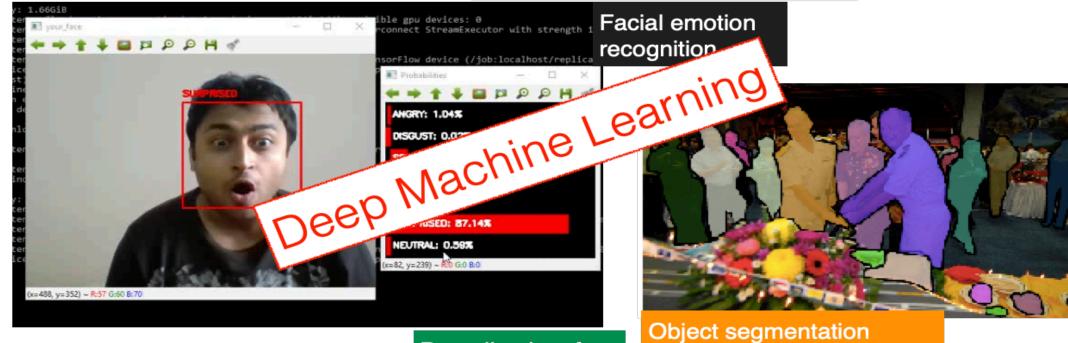
To realise human-like levels of cognition, Machine Learning solutions have to realise the above activities.

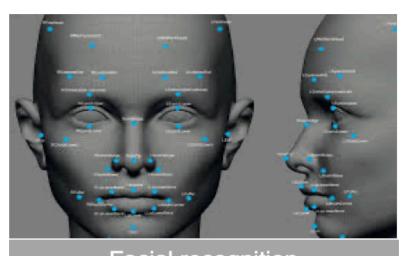
Machine Learning



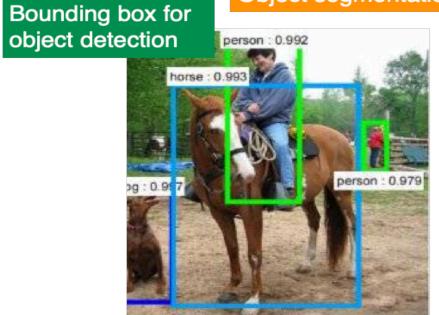


Single system teaches itself to master chess, shoji and go, using rules of the game.





Facial recognition

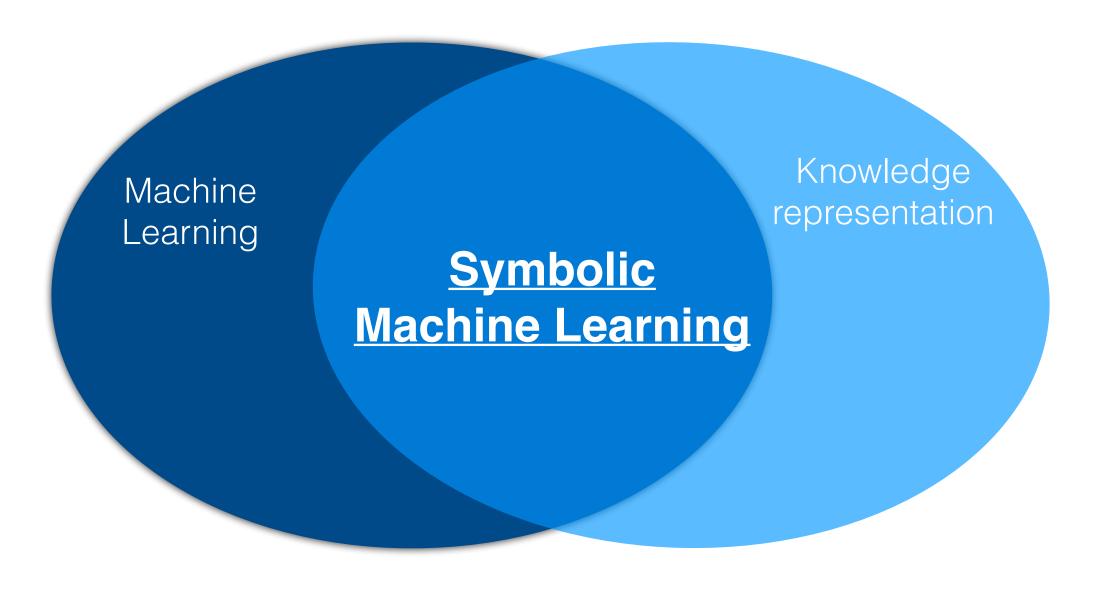


Advantages

- Ability to learn from unstructured data.
- Very effective in solving specific tasks, sometimes better than humans.

Drawbacks

- Data-intensive
- Inability to generalise
- Vulnerability to distributional shifts between training and test data
- Learned models are not interpretable
- Cannot use prior (or learned) knowledge



Information extraction from data
Predictions about unseen data
Ability to improve behaviour over time

Machine Learning

Symbolic Machine Learning

Machine Learning

Information extraction from data
Predictions about unseen data
Ability to improve behaviour over time

Symbolic Machine Learning

Machine

Learning

Knowledge

representation

Human-readable representation of knowledge

Rigorous inference mechanisms for making predictions

Can be automatically verified

Information extraction from data
Predictions about unseen data
Ability to improve behaviour over time

Machine Learning

Symbolic

Machine Learning

Knowledge representation

Human-readable representation of knowledge

Rigorous inference mechanisms for making predictions

Can be automatically verified



- learn from small amount of (noisy) dataset
- incorporate existing (partial) knowledge
- learn human-readable models
- support continuous and transfer learning

A symbolic machine learning task is a $T = \langle B, S_M, E^+, E^- \rangle$ and a Covers relation over T

В	Background knowledge
S _M	Set of possible solutions
E ⁺	Set of positive examples
E ⁻	Set of negative examples

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The goal is to find a solution H in S_M that explains the given examples:

- ► Covers(B, H, e) for every $e \in E^+$
- ▶ $\neg Covers(B, H, e)$ for every $e \in E^{-}$

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```
    Covers(B, H, e) for every e ∈ E<sup>+</sup>
    ¬Covers(B, H, e) for every e ∈ E<sup>-</sup>
```

Different notions of Covers relation define different symbolic machine learning frameworks.

```
E.g. B \cup H \models e for every e \in E^+
 B \cup H \not\models e for every e \in E^-
```

A symbolic machine learning task is a $T = \langle B, S_M, E^+, E^- \rangle$ and a Covers relation over T

	Background knowledge
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E ⁺	Set of positive examples
E-	Set of negative examples

```
B { parent(ann, mary). parent(ann, tom). parent(tom, eve). parent(tom, ian). female(ann). female(mary). female(eve) }

SM { daughter(X,Y) ← female(X). daughter(X,Y) ← parent(Y,X). daughter(X,Y) ← parent(Y,X), female(X) }

E+ { daughter(mary, ann). daughter(eve, tom) }

E- { daughter(tom, ann). daughter(eve, ann) }
```

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E- { daughter(tom, ann). daughter(eve, ann) }
```

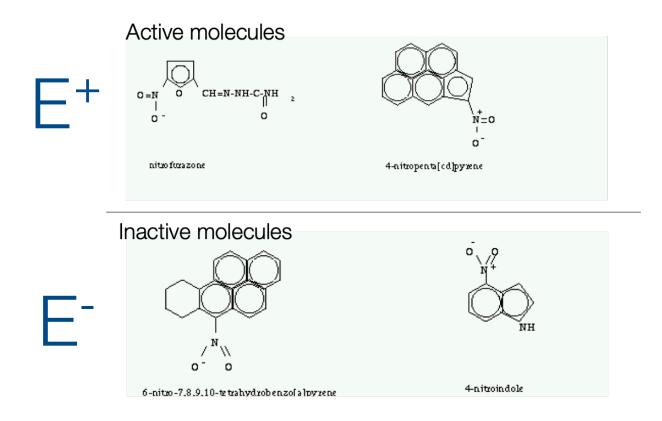
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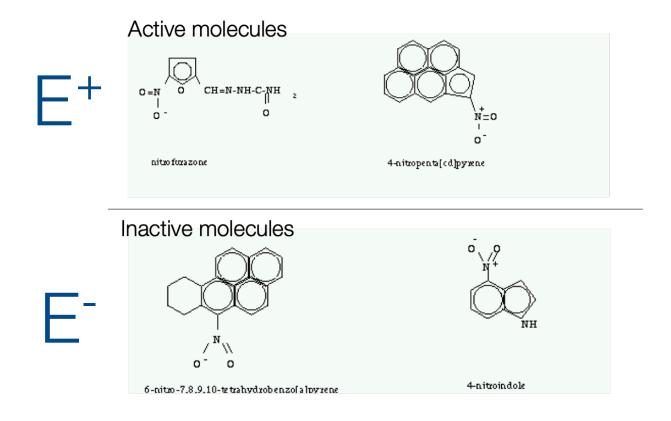
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E.g. B \cup H \models e \text{ for every } e \in E^+
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H = daughter(X,Y) \leftarrow parent(Y,X), female(X)
```

▶ Predict mutagenicity of nitro compounds, relevant for prediction of carcinogenesis



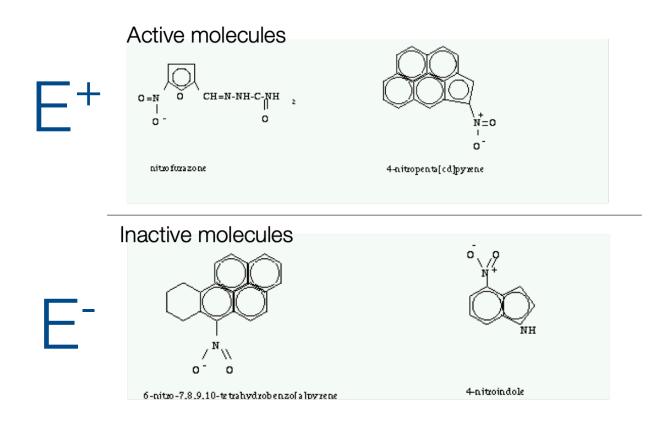
```
active(f1).
atom(f1, f1<sub>1</sub>, c, 21, 0.817).
atom(f1, f1<sub>2</sub>, c, 21, -0.143).
atom(f1, f1<sub>3</sub>, c, 21, -0.143).
.....
bond(f1, f1<sub>1</sub>, f1<sub>2</sub>, 7).
bond(f1, f1<sub>2</sub>, f1<sub>3</sub>, 7).
bond(f1, f1<sub>3</sub>, f1<sub>4</sub>, 7).
....
logmutag(f1, 0.64).
lumo(f1, -1.785).
logp(f1, 1.01).
ring_size5(f1, [f1<sub>5</sub>, f1<sub>1</sub>, f1<sub>2</sub>, f1<sub>3</sub>, f1<sub>4</sub>]).
```

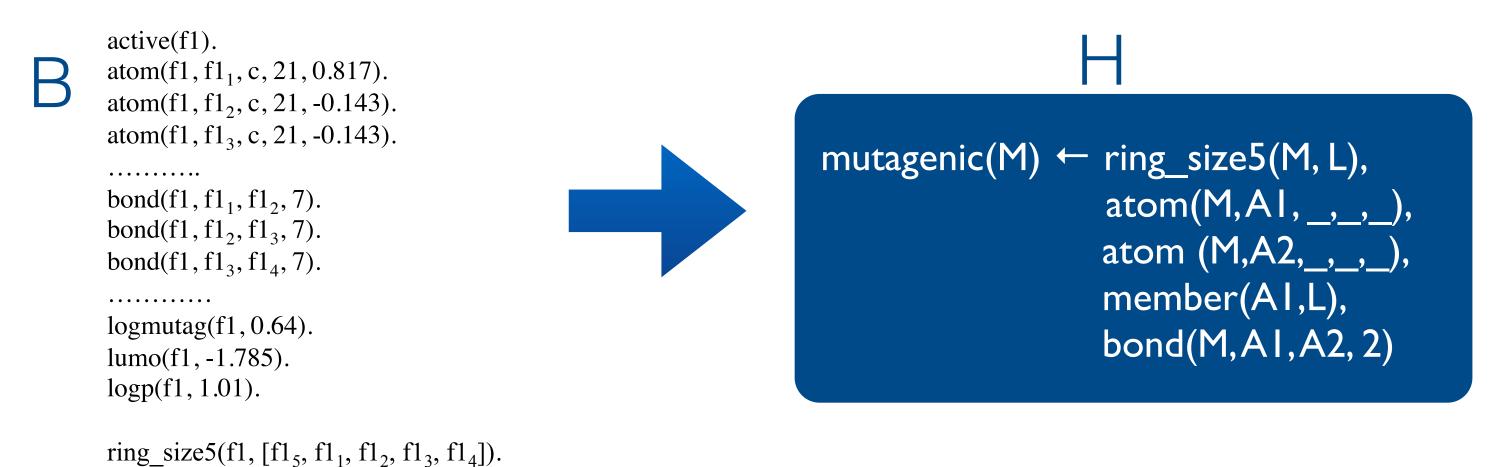
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```
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atom(f1, f1_1, c, 21, 0.817).
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                                                                                 mutagenic(M) \leftarrow ring\_size5(M, L),
bond(f1, f1<sub>1</sub>, f1<sub>2</sub>, 7).
                                                                                                                 atom(M, AI, __,__),
bond(f1, f1<sub>2</sub>, f1<sub>3</sub>, 7).
                                                                                                                atom (M,A2,__,_),
bond(f1, f1<sub>3</sub>, f1<sub>4</sub>, 7).
                                                                                                                member(AI,L),
logmutag(f1, 0.64).
                                                                                                                bond(M, A1, A2, 2)
lumo(f1, -1.785).
logp(f1, 1.01).
ring_size5(f1, [f1<sub>5</sub>, f1<sub>1</sub>, f1<sub>2</sub>, f1<sub>3</sub>, f1<sub>4</sub>]).
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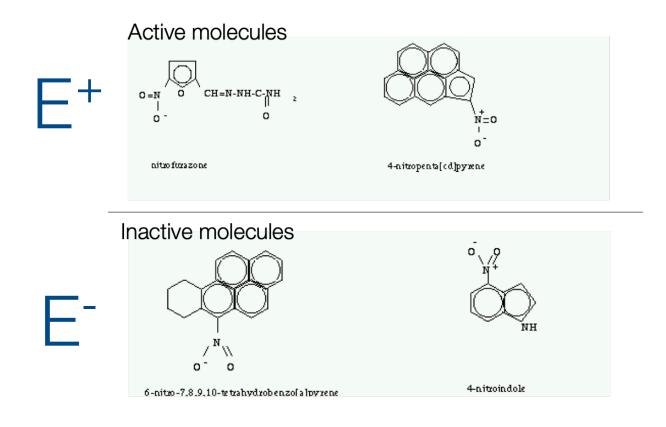
Learn regular grammars, from observations of positive and negative example strings

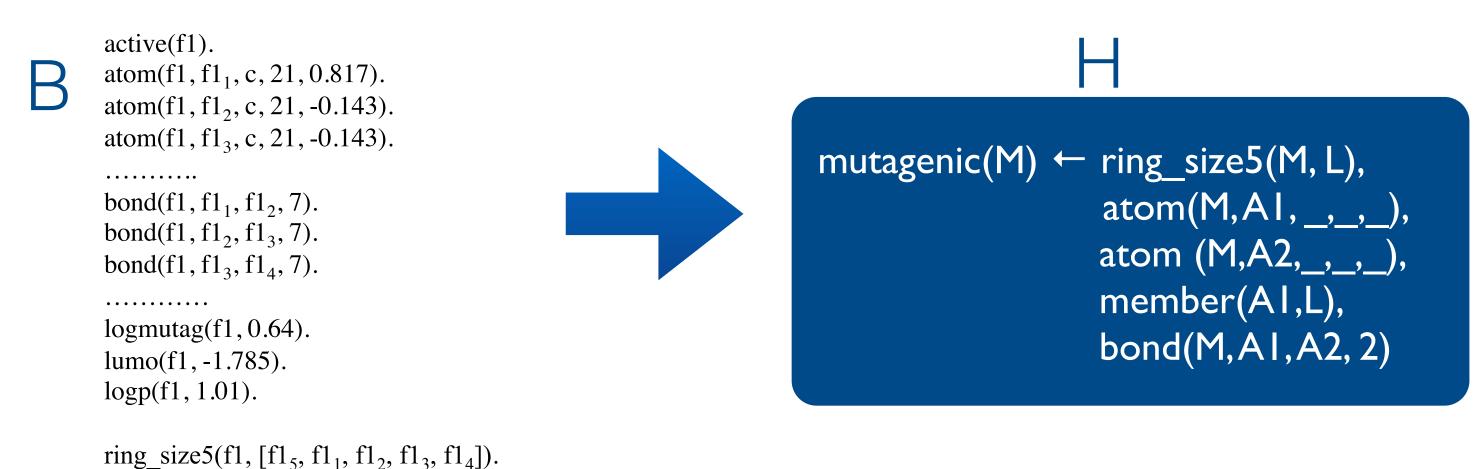
$$E^+ = s(0,3)$$

B
$$np(X,Y) \leftarrow word("She",X,Y).$$

 $mod(X,Y) \leftarrow word("quickly",X,Y).$
 $s(X,Y) \leftarrow np(X,Z), vp(Z,Y).$
 $vp(X,Y) \leftarrow v(X,Y).$
word("She",0,1)
 $word("quickly", 2,3)$
 $word(ran,1,2)$
 $\leftarrow v(1,3)$

▶ Predict mutagenicity of nitro compounds, relevant for prediction of carcinogenesis



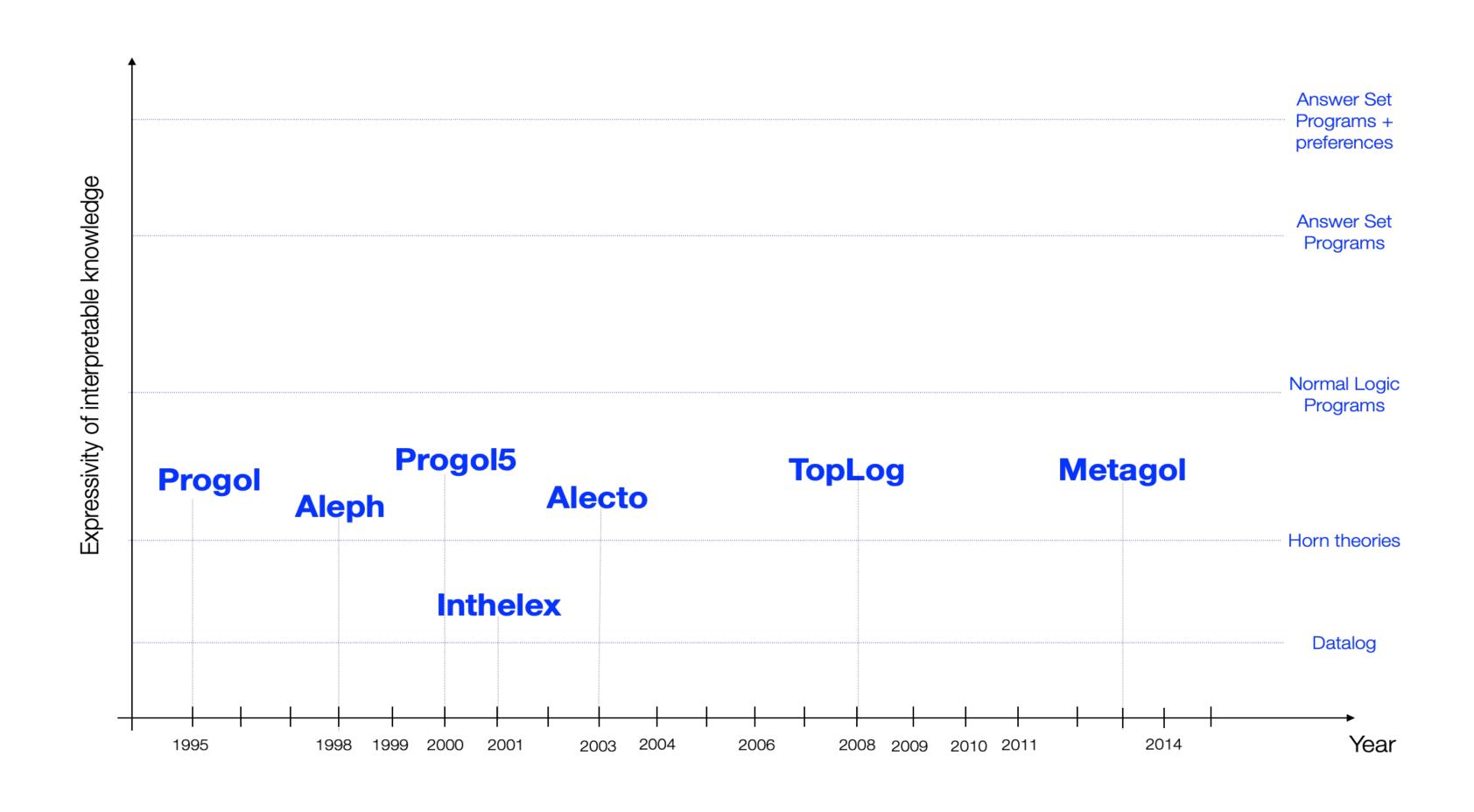


Learn regular grammars, from observations of positive and negative example strings

$$E^+ = s(0,3)$$

 $\begin{array}{l} & \text{np}(X,Y) \leftarrow \text{word}(\text{``She''},X,Y). \\ & \text{mod}(X,Y) \leftarrow \text{word}(\text{``quickly''},X,Y). \\ & \text{s}(X,Y) \leftarrow \text{np}(X,Z), \text{vp}(Z,Y). \\ & \text{vp}(X,Y) \leftarrow \text{v}(X,Y). \\ & \text{word}(\text{``She''},0,1) \\ & \text{word}(\text{``quickly''},2,3) \\ & \text{word}(\text{ran},1,2) \\ & \leftarrow \text{v}(1,3) \end{array} \end{array}$

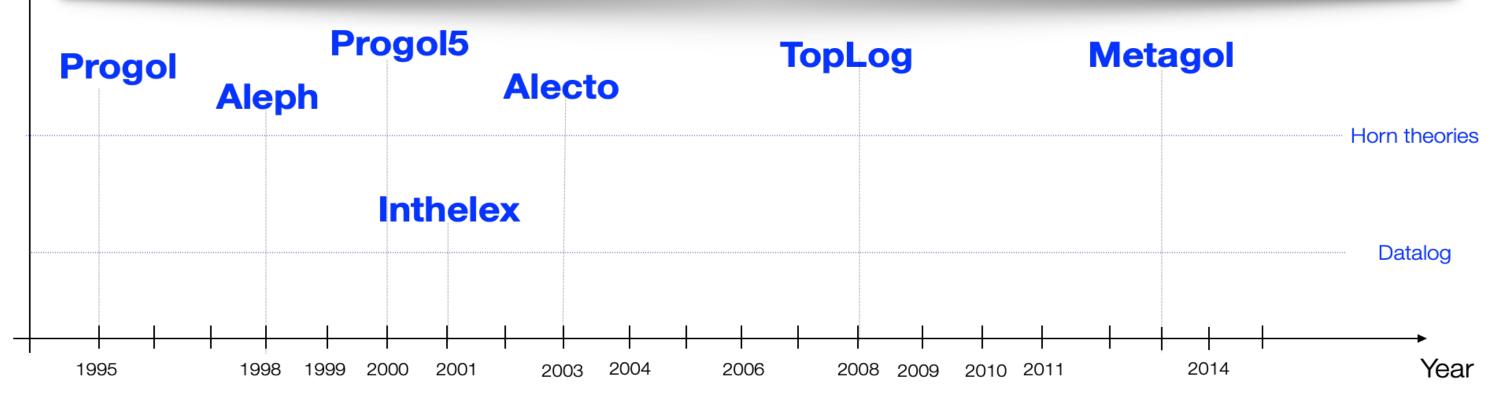
Early algorithms and systems



Early algorithms and systems

Three Main Misconceptions:

- Models expressing recursive concepts, non-monotonic assumptions, constraints, preferences, are thought to be too complex to be efficiently learned by a general purpose symbolic machine learning algorithm.
- Symbolic machine learning is not robust to noise in the data.
- Symbolic machine learning is not scalable to large datasets and large search spaces.



Expressivity of interpretable knowledge

Learning complex but interpretable models

Behaving autonomously in the real-world requires learning default assumptions

succeeds(putdown, T) ← not happened(move(loc1,loc2),T-2)



Learning complex but interpretable models

Behaving autonomously in the real-world requires learning default assumptions

```
succeeds(putdown, T) ← not happened(move(loc1,loc2),T-2)
```

 Guaranteeing correct and safe decisions require learning constraints

```
falsity ← value(V, C1), value(V, C2), same_col(C1, C2).

falsity ← value(V, C1), value(V, C2), same_row(C1, C2).

falsity ← value(V, C1), value(V, C2), same_block(C1, C2).
```



0	6	2	1	0	7	0	8	0
								0
8	D	0	0	0	4	0	0	0
						1.0		0
4	9	l	0	6	0	O	2	8
5	0	0	3	4	0	/	0	0
								0
								0
0	5	0	0	0	0	9	6	6

Learning complex but interpretable models

Behaving autonomously in the real-world requires learning default assumptions

succeeds(putdown, T) \leftarrow not happened(move(loc1,loc2),T-2)



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falsity ← value(V, C1), value(V, C2), same_block(C1, C2).
```

Assisting humans in their decision making require learning their preferences

```
:~ mode(Zone, walk), crime_rating(Zone, R), R > 4.[1@3]
```

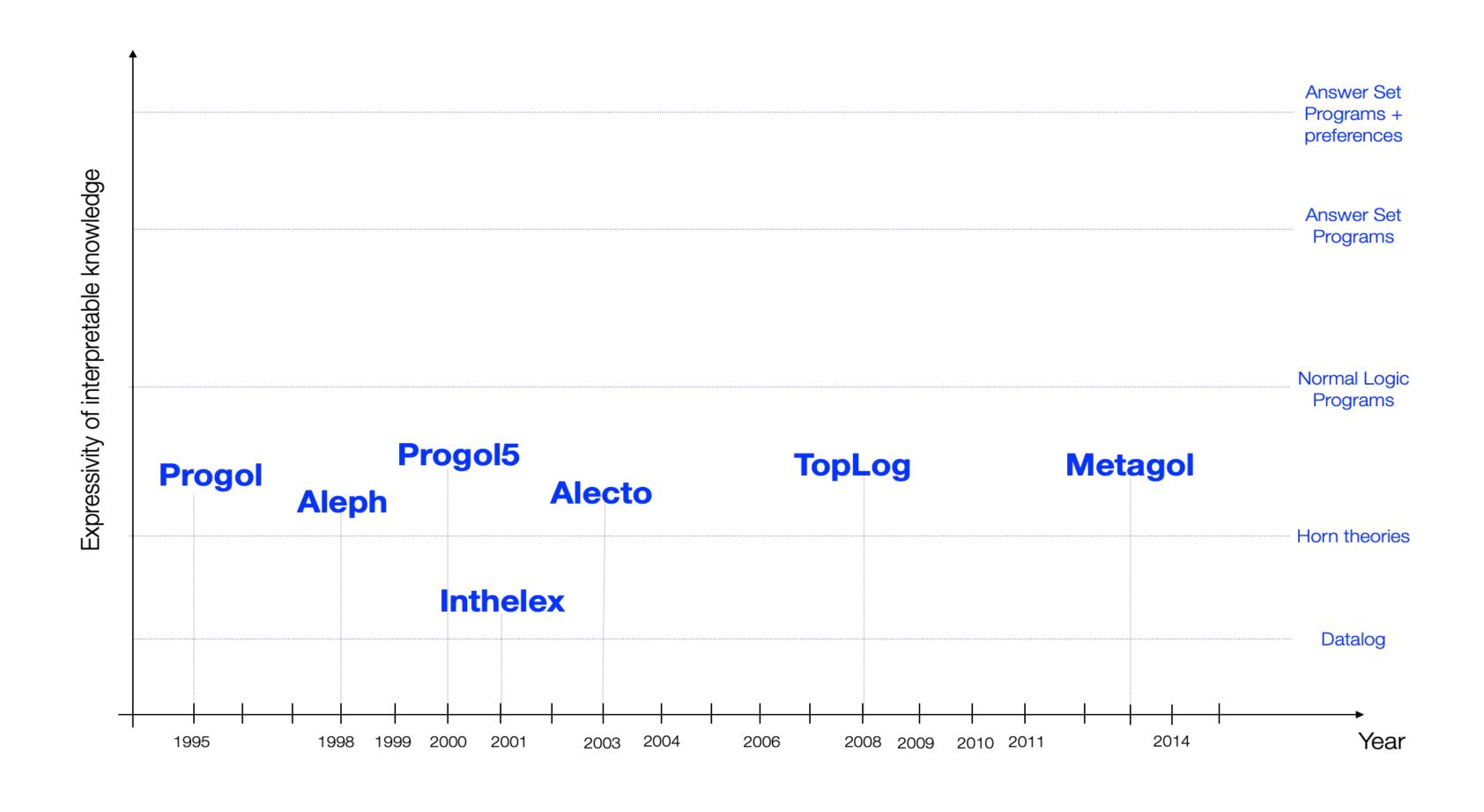
:~ mode(Zone, bus).[1@2]

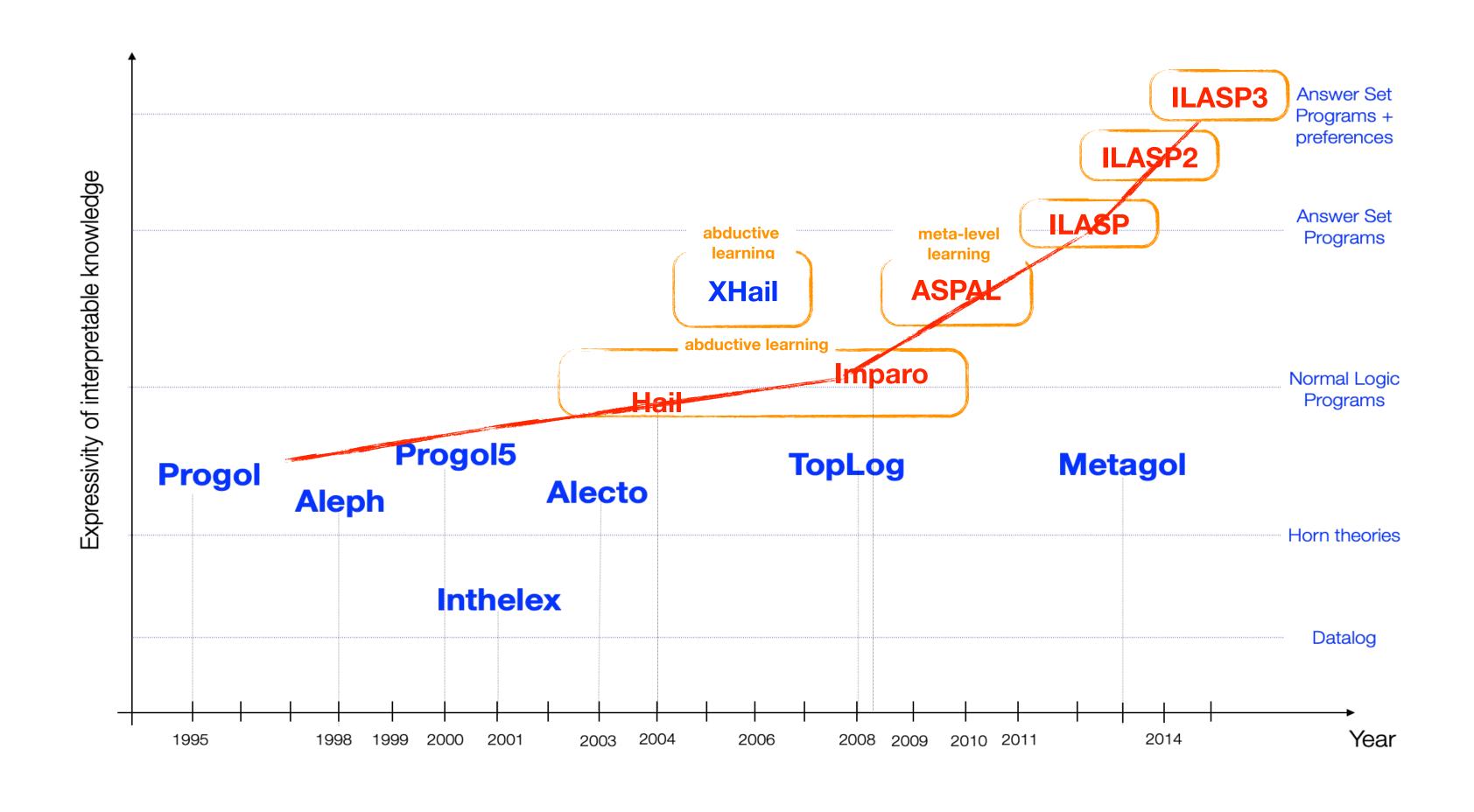
:~ mode(Zone, walk), distance(Zone, D).[D@1]

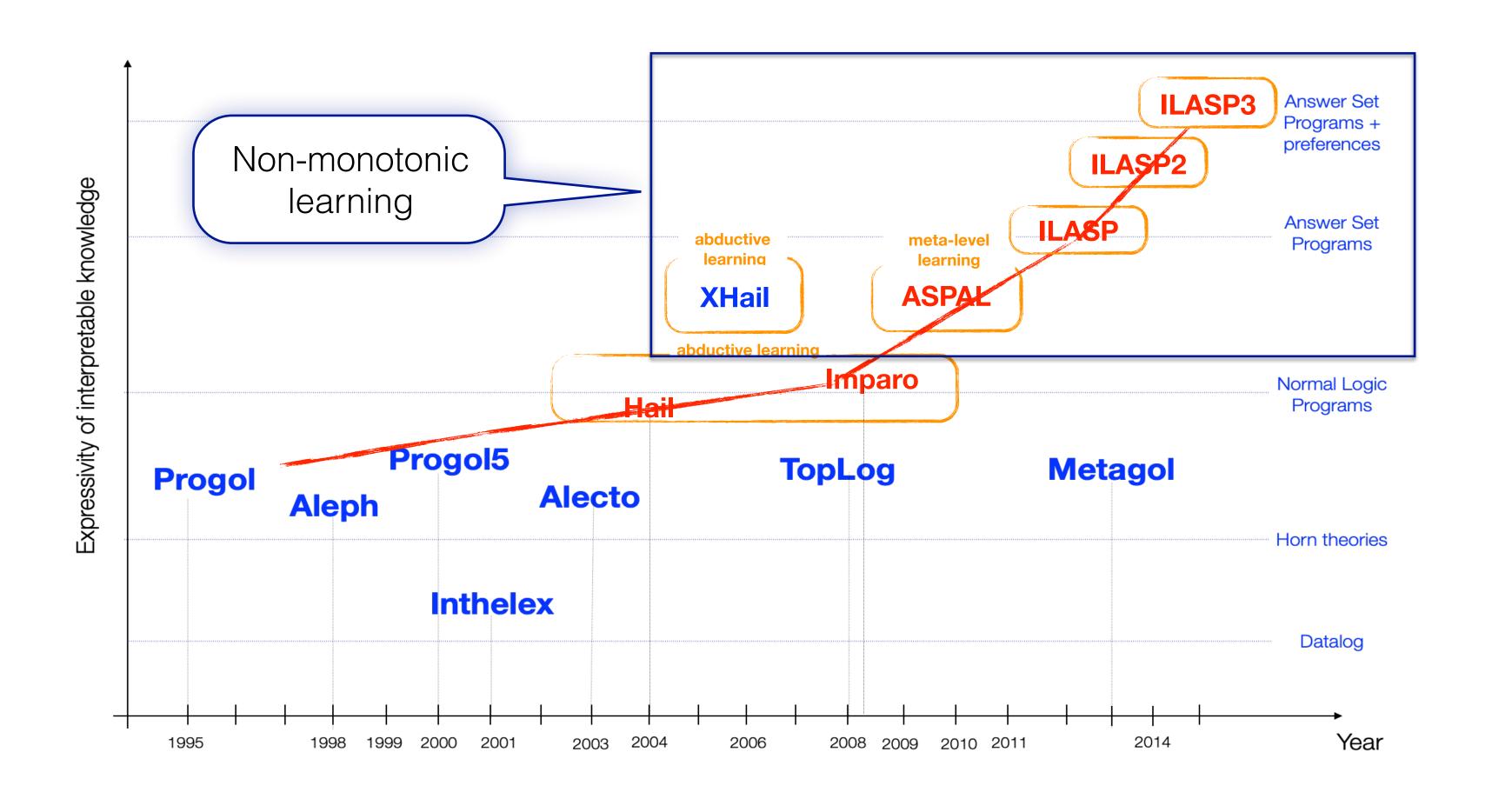


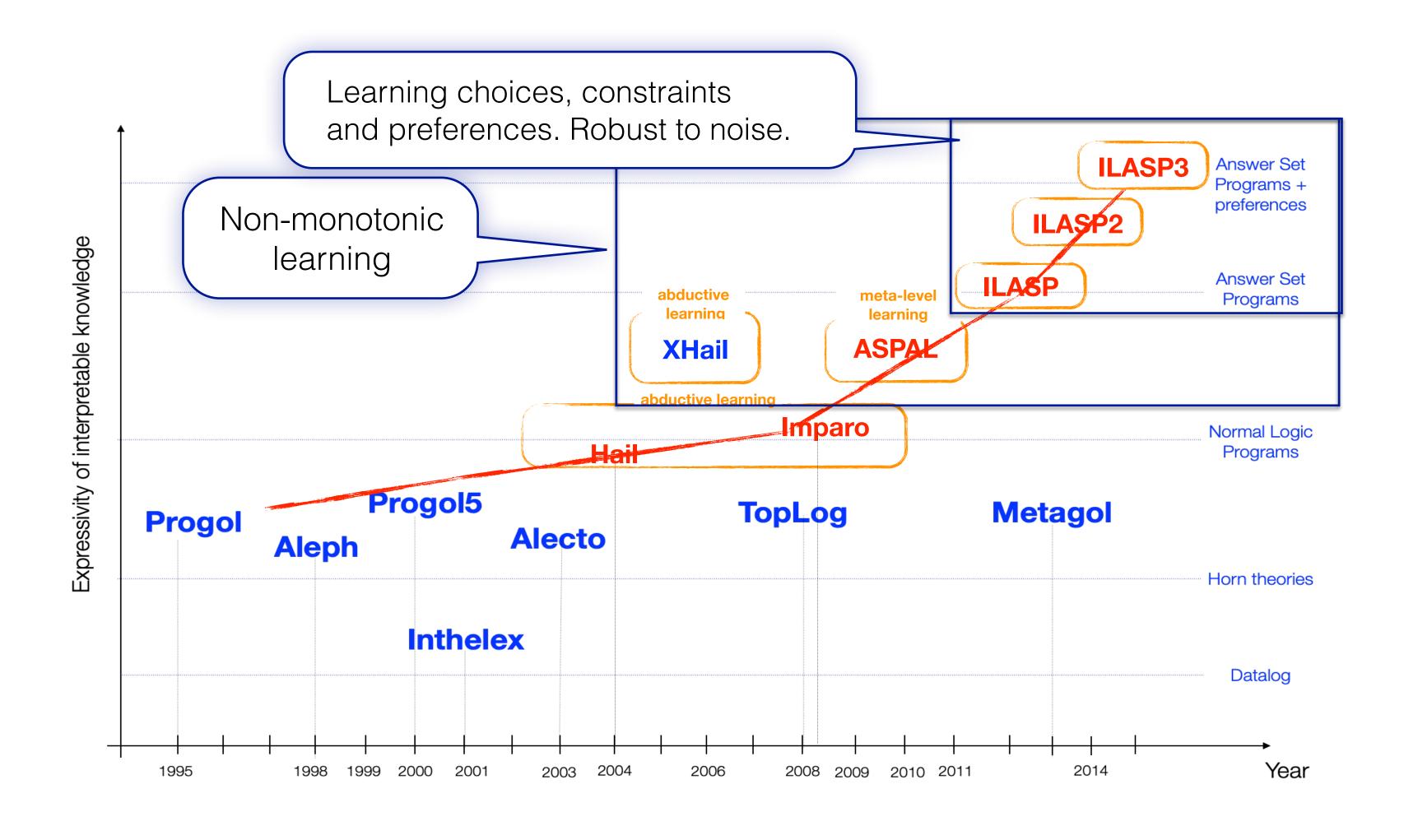
0	6	2	1	0	7	0	8	O
			0					
8	D	0	0	0	4	0	0	0
0	0	0	0	8	0	7	0	0
4	9	t	0	6	0	O	2	8
5	0	0	ფ	4	0	/	0	0
			Ø					
1	7	0	0	0	0	J	0	0
0	5	0	0	0	0	4	6	6







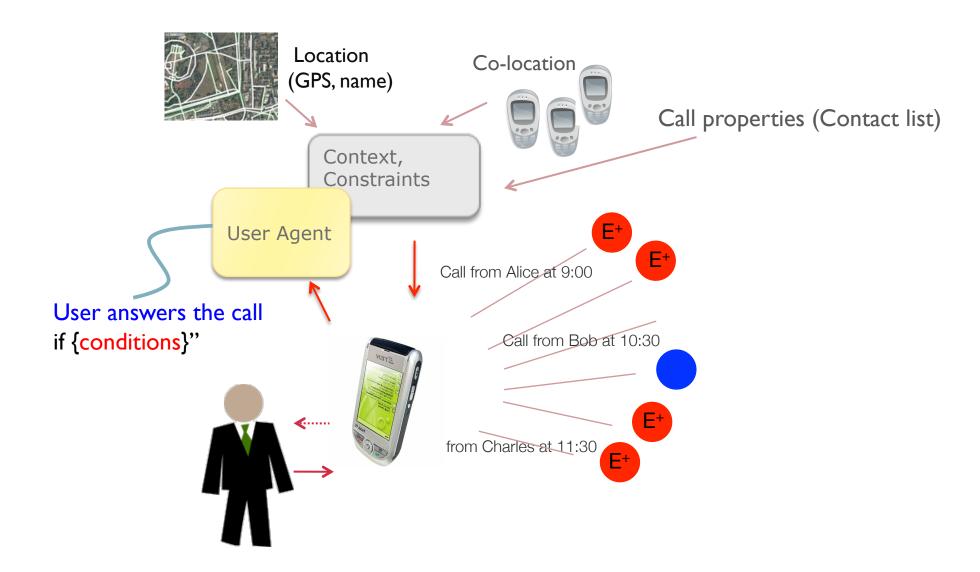




Learning Rule-based Policies

Learning user behaviour models in pervasive systems

- Devices are able to continuously learn policies from (user) past actions
- Learned policies are used to automatically adapt their behaviours and reduce human intervention

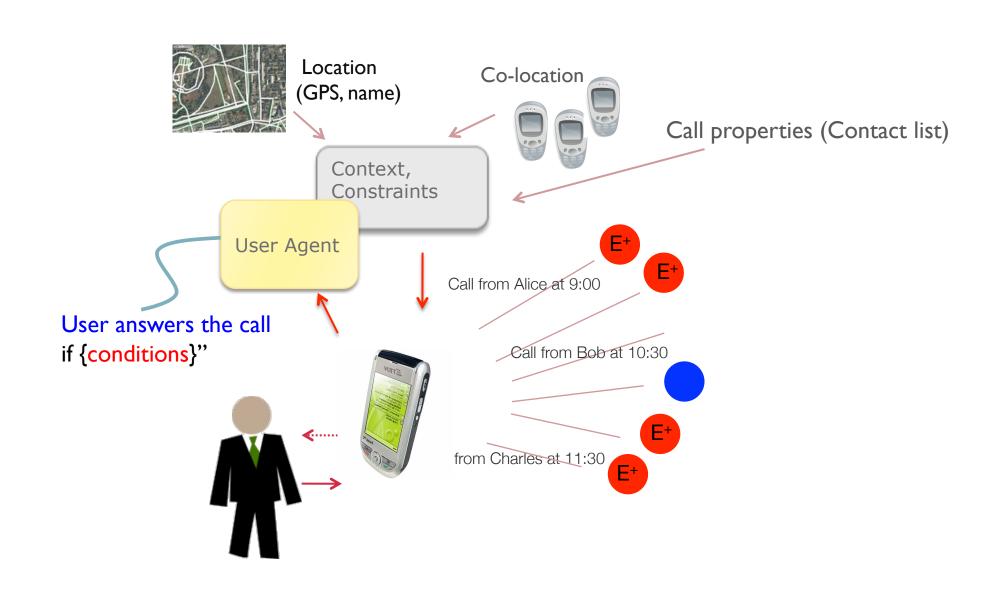


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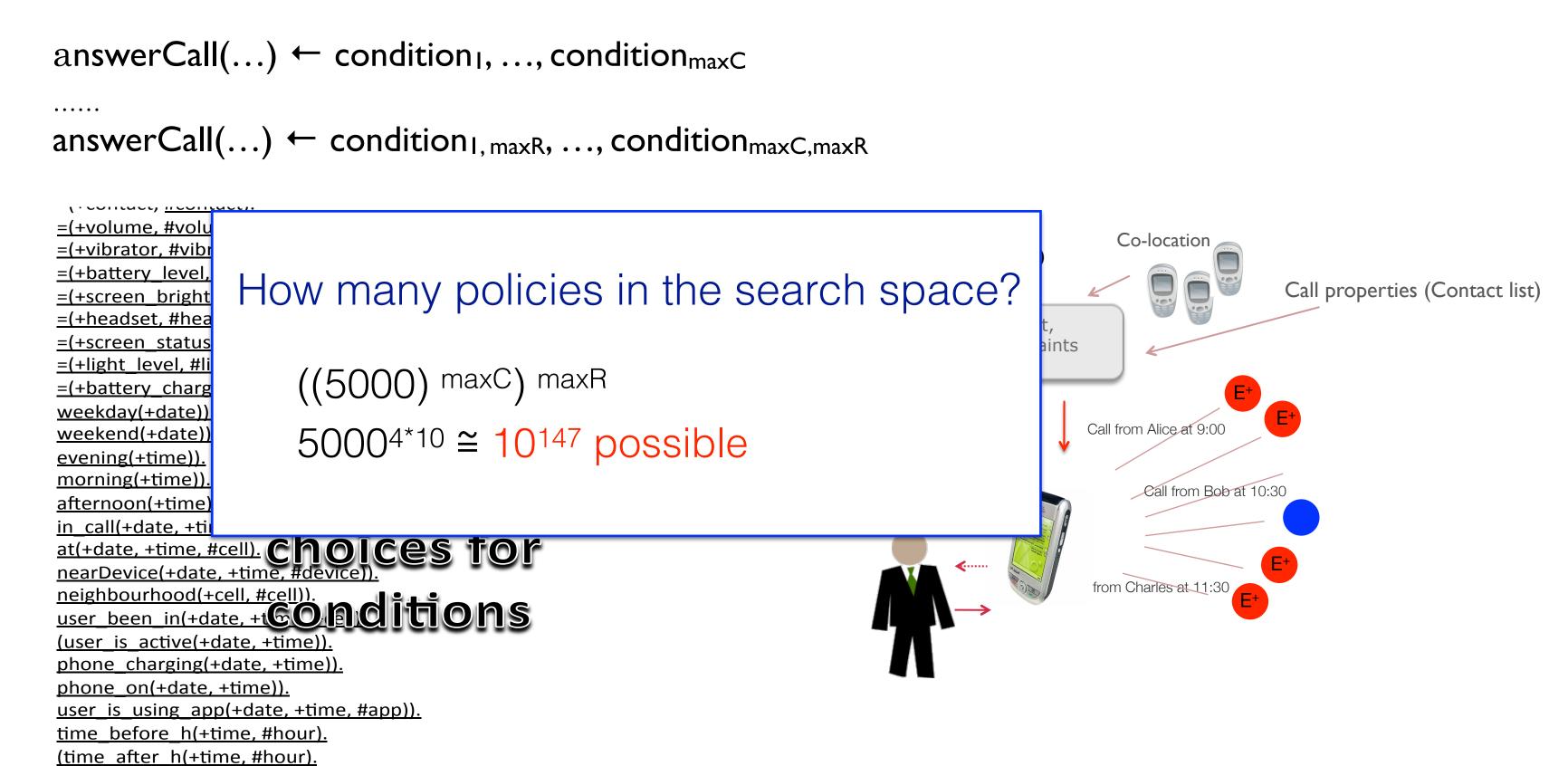
```
answerCall(...) ← condition<sub>1</sub>, ..., condition<sub>maxC</sub>
answerCall(...) \leftarrow condition<sub>1, maxR</sub>, ..., condition<sub>maxC,maxR</sub>
 =(+volume, #volume).
=(+vibrator, #vibrator)
 =(+battery level, #battery level).
 =(+screen brightness, #screen brightness).
 =(+headset, #headset).
 =(+screen status, #screen status).
=(+light level, #light level).
 =(+battery charging, #battery charging).
weekday(+date)).
weekend(+date)).
 evening(+time)).
                      Around 5000
morning(+time)).
afternoon(+time)).
 in call(+date, +time))
at(+date, +time, #cell).
 neighbourhood(+cell, #cell)
phone charging(+date, +time))
phone_on(+date, +time)).
user is using app(+date, +time, #app)).
time before h(+time, #hour).
(time after h(+time, #hour).
```



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user is using app(+date, +time, #app)).

time before h(+time, #hour).

(time after h(+time, #hour).

Learning Rule-based Policies

Learning user behaviour models in pervasive systems

- Devices are able to continuously learn policies from (user) past actions
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ASPAL

```
answerCall(...) \leftarrow condition<sub>1</sub>, ..., condition<sub>maxC</sub>
answerCall(...) \leftarrow condition<sub>1, maxR</sub>, ..., condition<sub>maxC,maxR</sub>
 <u>=(+volume, #volu</u>
                                                                                                               Co-location
=(+vibrator, #vibr
=(+battery_level,
                   How many policies in the search space?
                                                                                                                                Call properties (Contact list)
=(+screen_bright
=(+headset, #hea
 =(+screen status
=(+light level, #li
                         ((5000) maxC) maxR
 =(+battery charg
weekday(+date))
                                                                                                            Call from Alice at 9:00
                         5000^{4*10} \cong 10^{147} possible
weekend(+date)
 evening(+time)).
morning(+time))
 afternoon(+time)
 in call(+date, +til
at(+date, +time, #cell). Choices for nearDevice(+date, +time, #device)).
 neighbourhood(+cell, #cell))
 phone charging(+date, +time))
phone_on(+date, +time)).
```



phone_on(+date, +time)).

time before h(+time, #hour).

(time after h(+time, #hour).

user is using app(+date, +time, #app)).

Learning Rule-based Policies

Learning user behaviour models in pervasive systems

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answerCall(...) ← condition₁, ..., condition_{maxC} answerCall(...) \leftarrow condition_{1, maxR}, ..., condition_{maxC,maxR} <u>=(+volume, #volu</u> Co-location =(+vibrator, #vibr =(+battery_level, How many policies in the search space? Call properties (Contact list) =(+screen bright =(+headset, #hea =(+screen status =(+light level, #li ((5000) maxC) maxR =(+battery charg weekday(+date)) Call from Alice at 9:00 $5000^{4*10} \cong 10^{147}$ possible weekend(+date) evening(+time)). morning(+time)) afternoon(+time) at(+date, +time, #cell). Choices for nearDevice(+date, +time, #device)). neighbourhood(+cell, #cell)) phone charging(+date, +time))

ASPAL

Imperial College London

Inductive Learning of Answer Set Programs

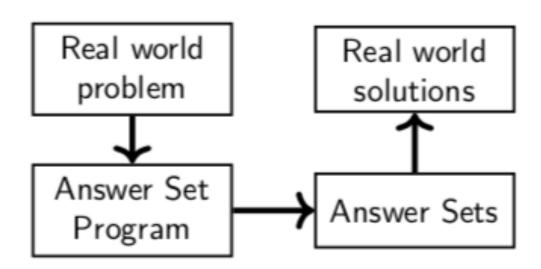
The ILASP Systems



The ILASP Systems

Answer Set Programming

Expressive Declarative Environment for Reasoning Logically

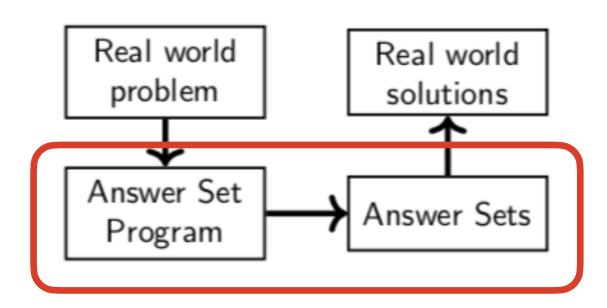




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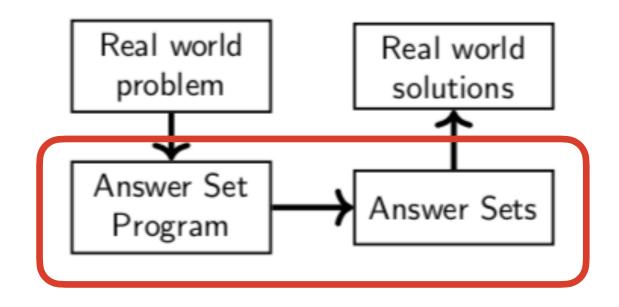




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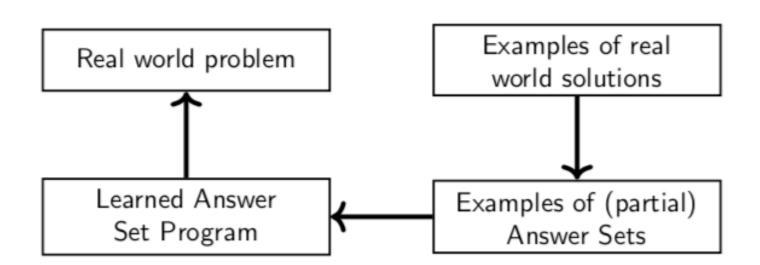
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ILASP

Expressive Declarative Environment for Learning Logically

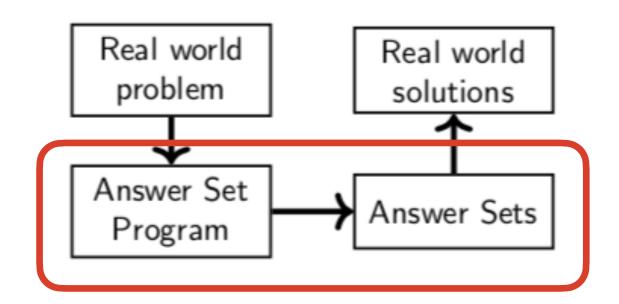




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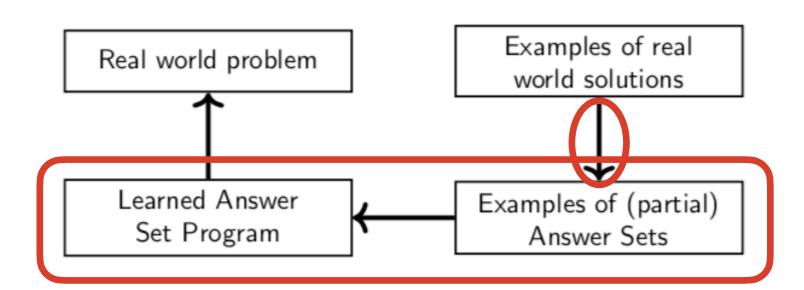
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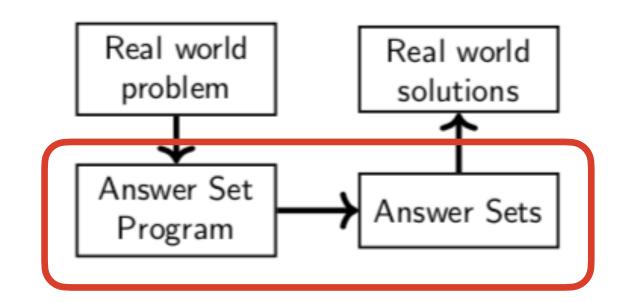




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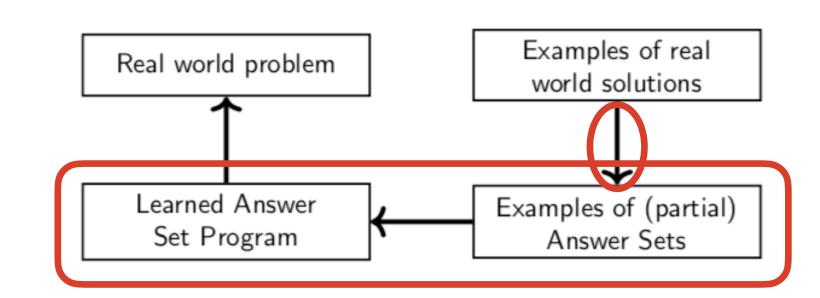
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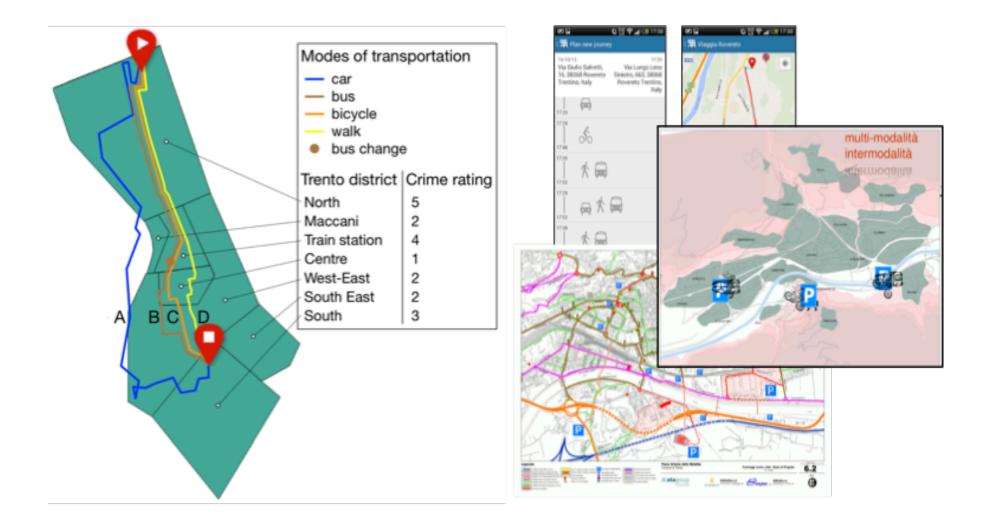
Desirable features for expressing (learned) knowledge in cognitive systems:

- Defaults and exceptions can be modelled using <u>negation as failure</u>
- Non-determinism and choice can modelled using choice rules
- Preferences can be modelled using weak constraints



Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Intelligent Urban Mobility System





ILASP2



Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Intelligent Urban Mobility System







ILASP2

Suggest user different alternatives:

- Walk 2km through an area with crime rating of 2.
- Take the bus 3km through an area with crime rating 4.

Journey B

- Take the bus 4km through an area with crime rating of 2
 Walk 1km through
- Walk 1km through an area with crime rating 5.

Journey C

- Take the bus 400m through an area with crime rating of 2.
- Take a second bus
 3km through an area
 with crime rating 4

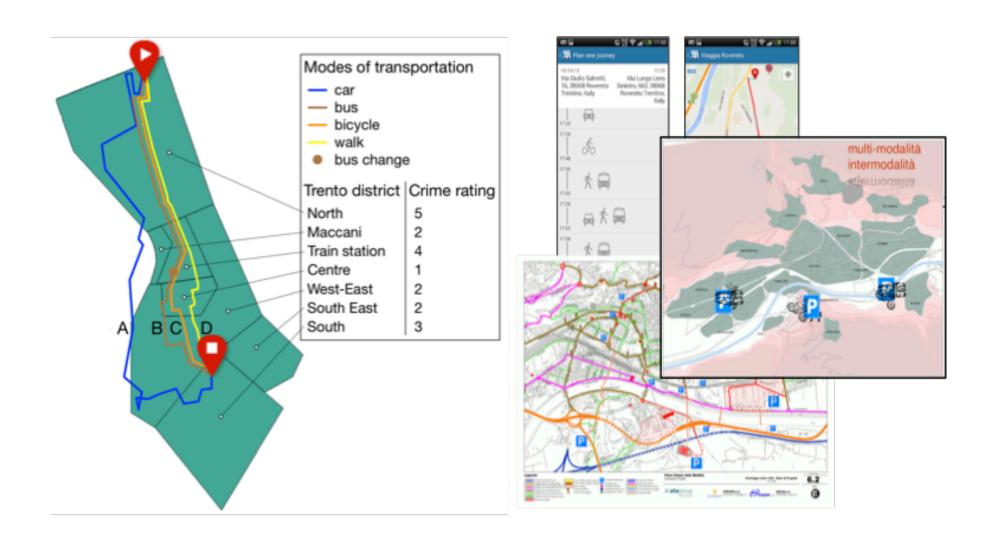
Journey D

- Take a bus 2km through an area with crime rating 5.
- Walk 2km through an area with crime rating 1.



Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Intelligent Urban Mobility System







ILASP2

Suggest user different alternatives:

- Walk 2km through an area with crime rating of 2.
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- Take the bus 4km through an area with crime rating of 2
- Walk 1km through an area with crime rating 5.

Journey C

- Take the bus 400m through an area with crime rating of 2.
- Take a second bus3km through an areawith crime rating 4

Journey D

- Take a bus 2km through an area with crime rating 5.
- Walk 2km through an area with crime rating 1.

Generate counter-examples

Journey A

- Walk 2km through an area with crime rating of 2.
- Take the bus 3km through an area with crime rating 4.

>

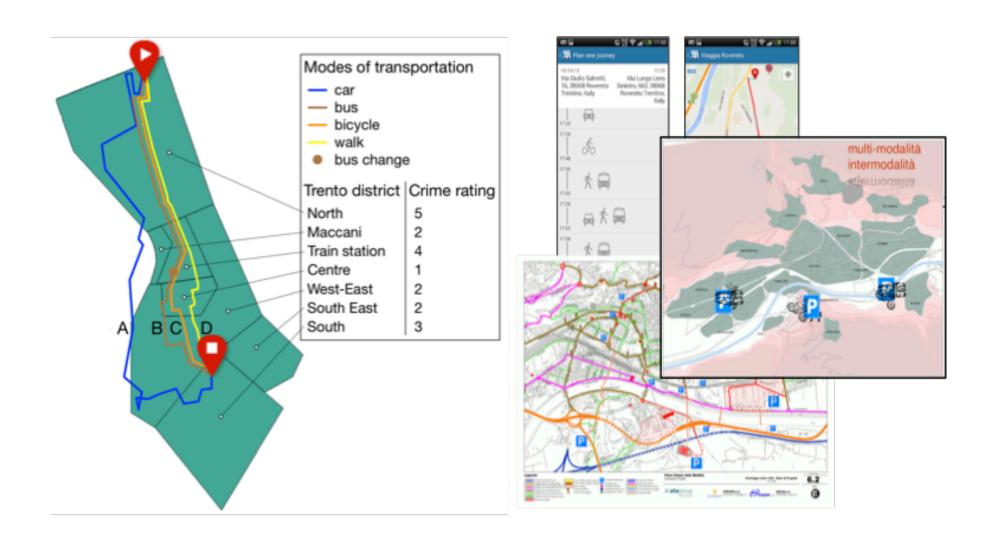
- Journey B
- Take the bus 4km through an area with crime rating of 2
- •Walk 1km through an area with crime rating 5.

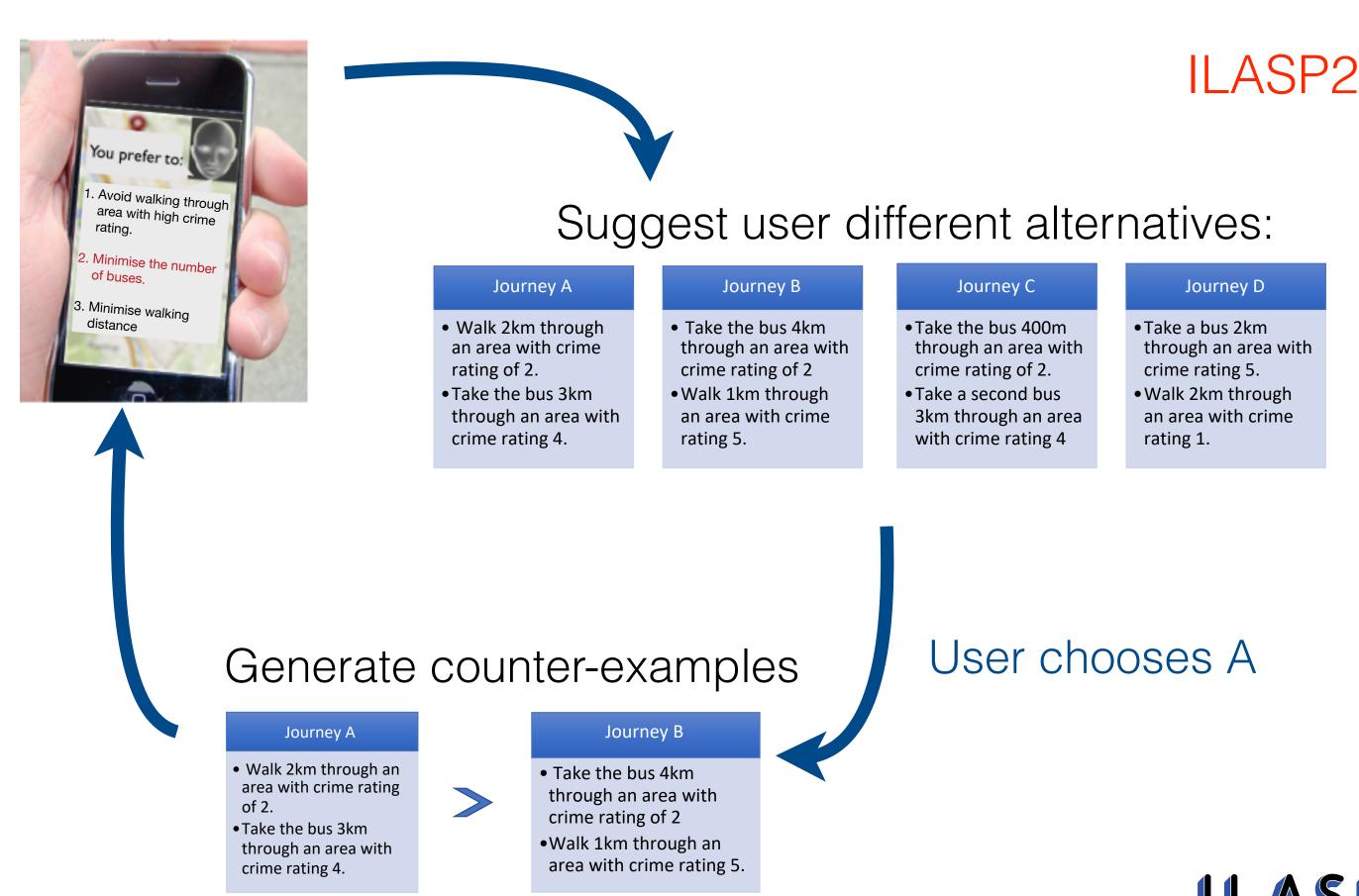
User chooses A



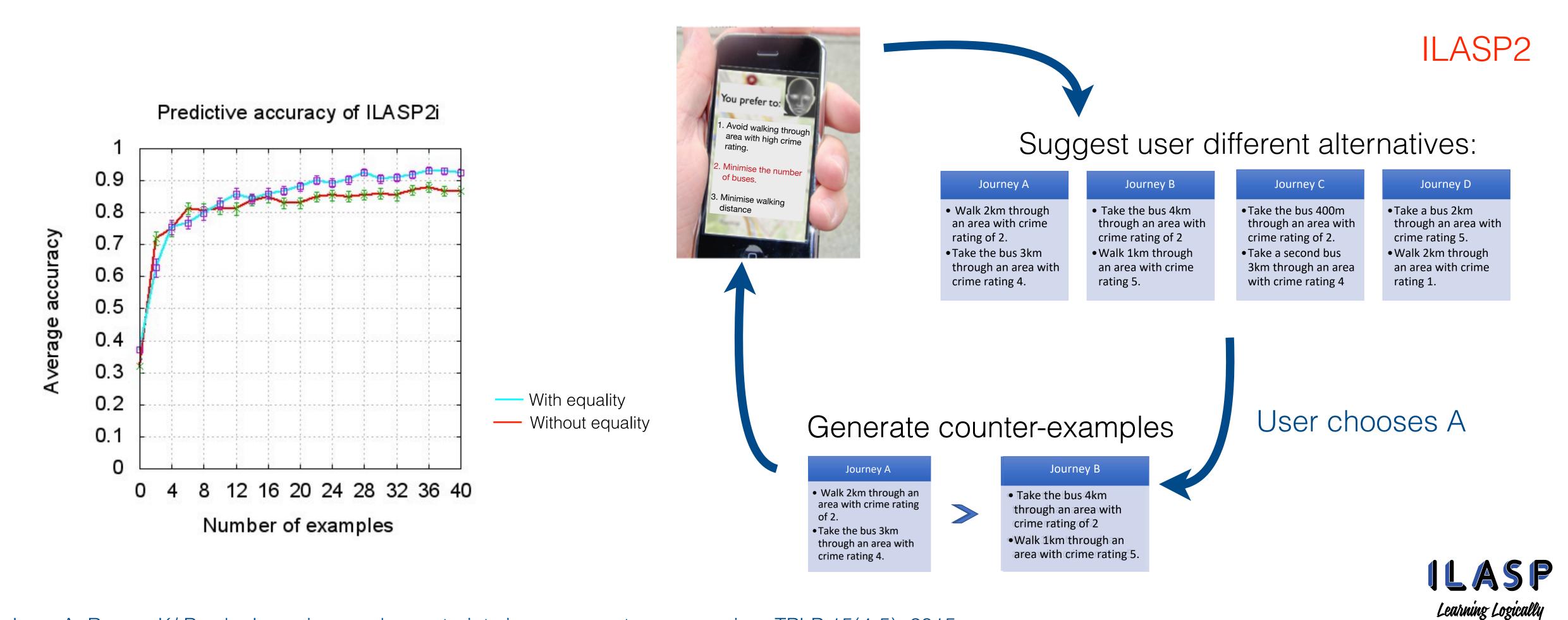
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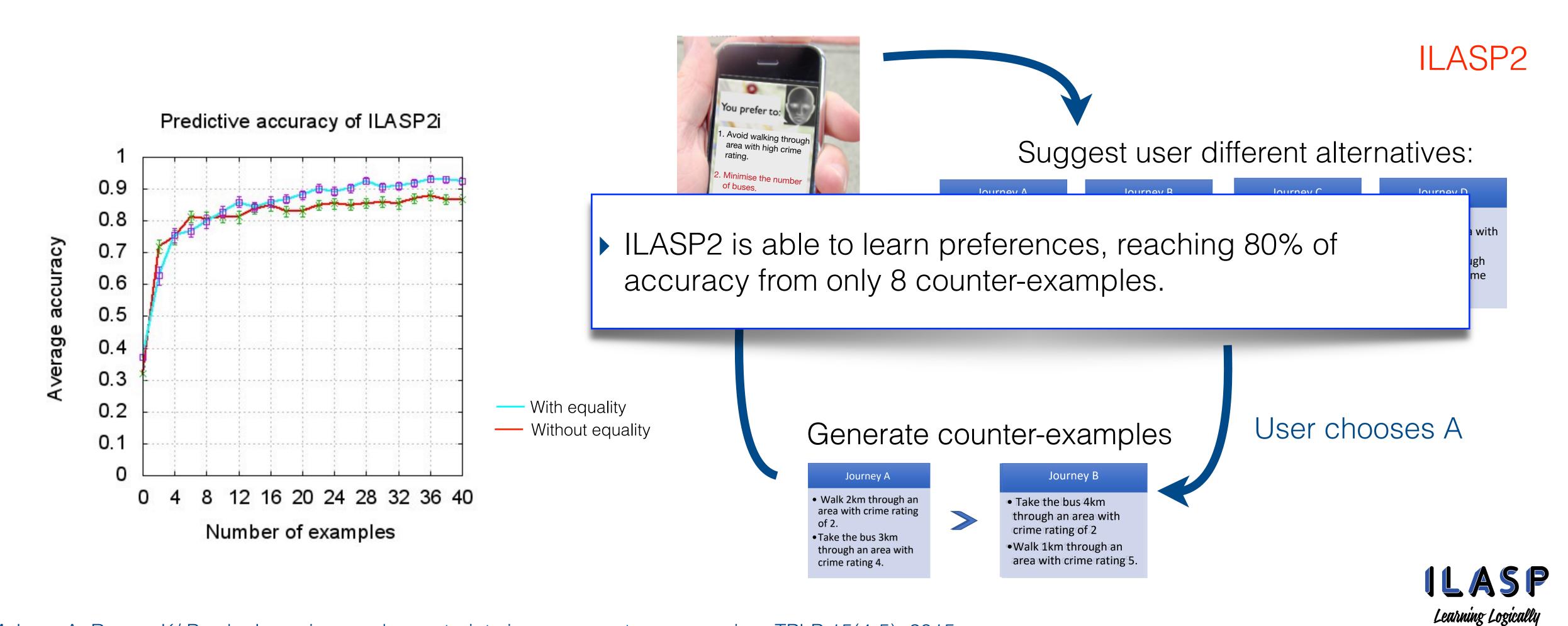




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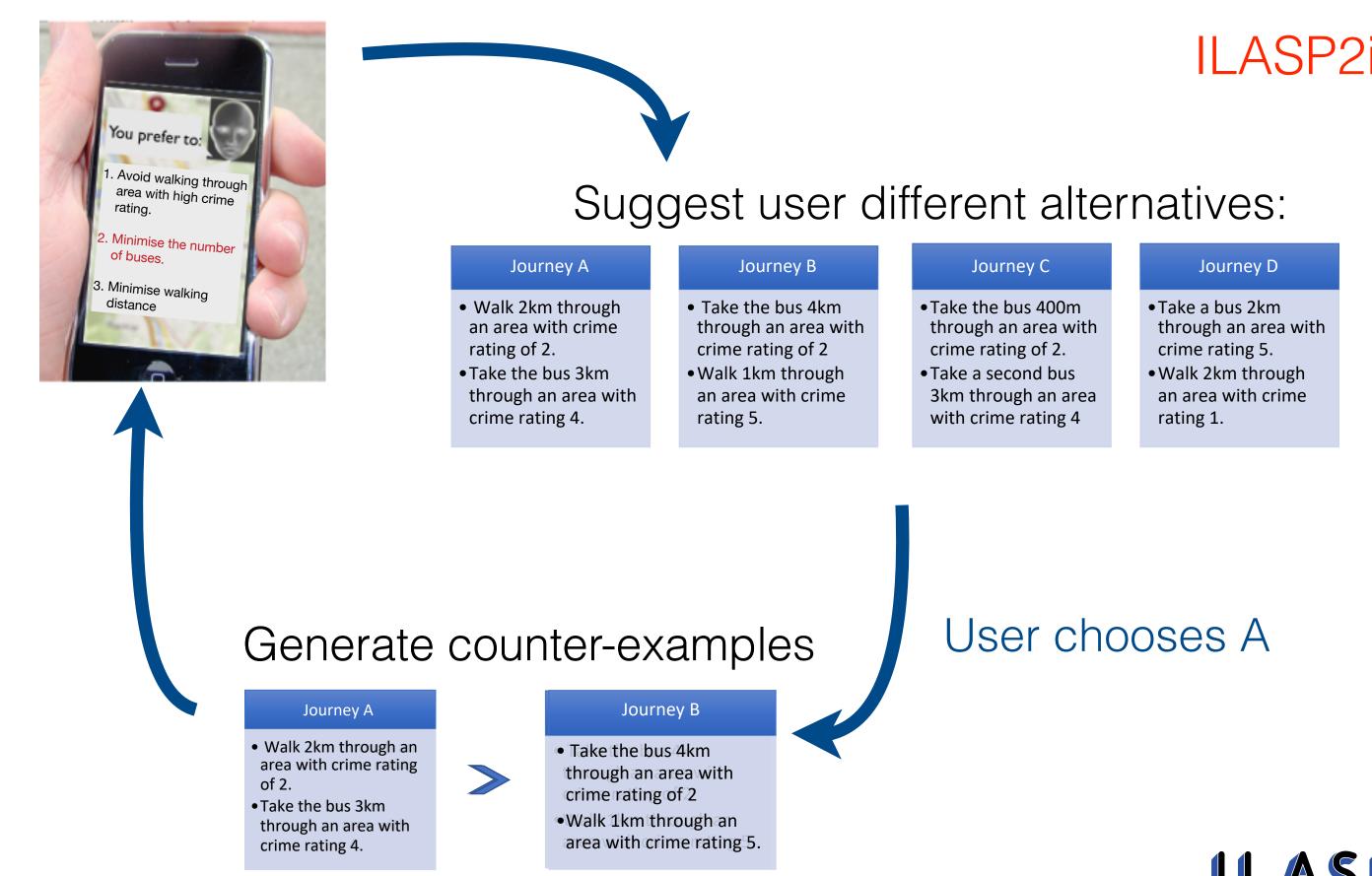


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To scale up the number of counter-examples, context-dependent counter-examples can be considered.





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To scale up the number of counter-examples, context-dependent counter-examples can be considered.

if it is not raining

Journey A

- Walk 2km through an area with crime rating
- Take the bus 3km through an area with crime rating 4.



- Take the bus 4km through an area with crime rating of 2
 - Walk 1km through an area with crime rating 5.

Journey B

if it is raining

Journey A

- Walk 2km through an area with crime rating
- Take the bus 3km through an area with crime rating 4.



- Take the bus 4km through an area with crime rating of 2
- •Walk 1km through an area with crime rating 5.

Journey B





- Walk 2km through an area with crime
- rating of 2. • Take the bus 3km through an area with crime rating 4.

Journey A

Journey B

- Take the bus 4km through an area with crime rating of 2
- Walk 1km through an area with crime rating 5.

Journey C

Suggest user different alternatives:

- Take the bus 400m through an area with crime rating of 2.
- Take a second bus 3km through an area with crime rating 4

Journey D

ILASP2i

- Take a bus 2km through an area with crime rating 5.
- Walk 2km through an area with crime rating 1.

Generate counter-examples

Journey A

- Walk 2km through an area with crime rating
- Take the bus 3km through an area with crime rating 4.

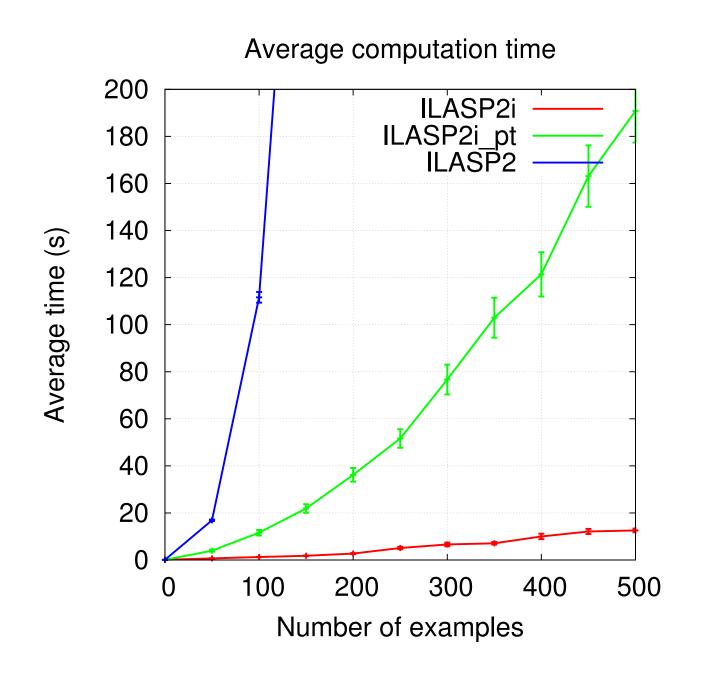
- Journey B
- Take the bus 4km through an area with crime rating of 2
- Walk 1km through an area with crime rating 5.

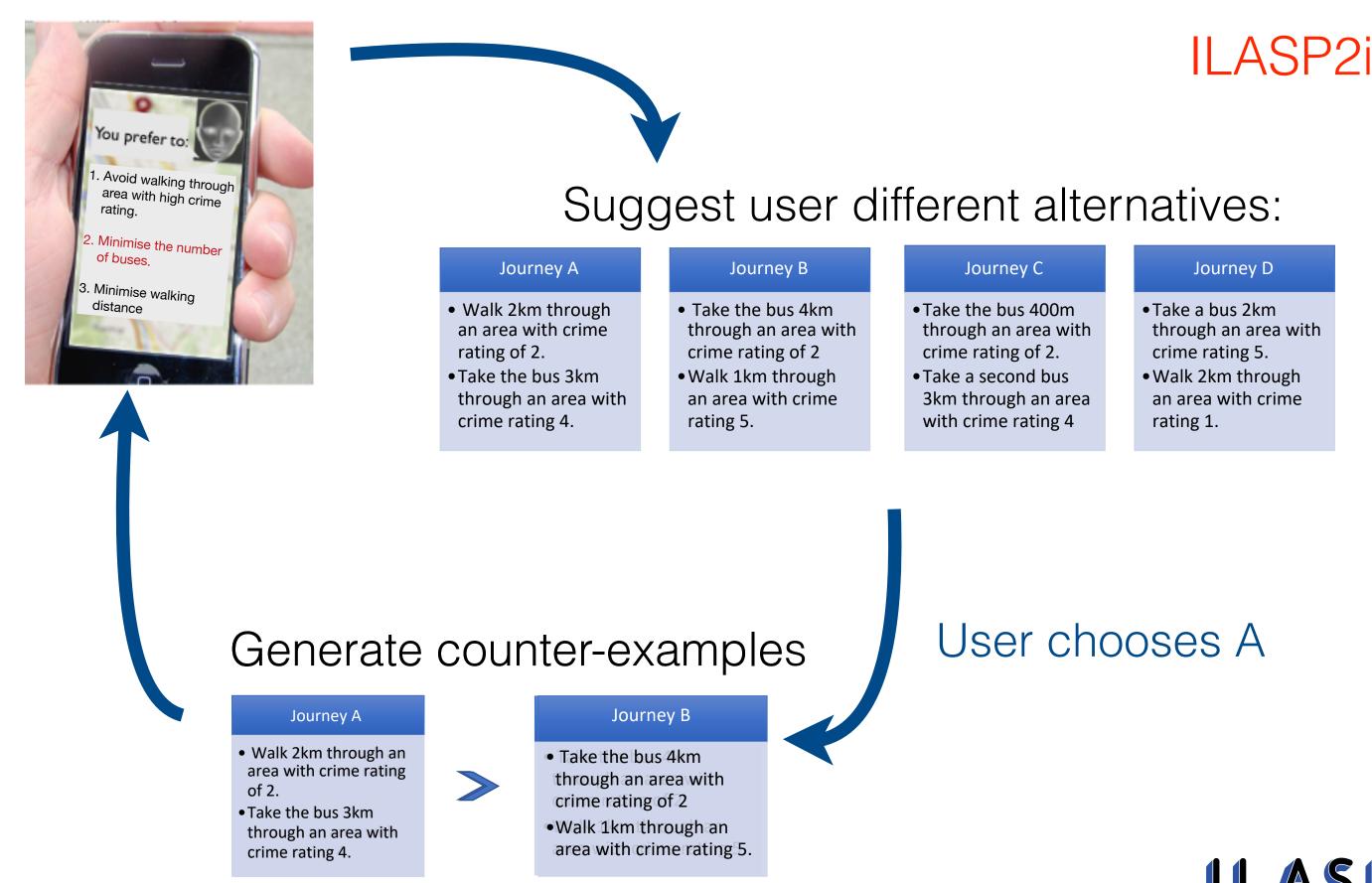
User chooses A



Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

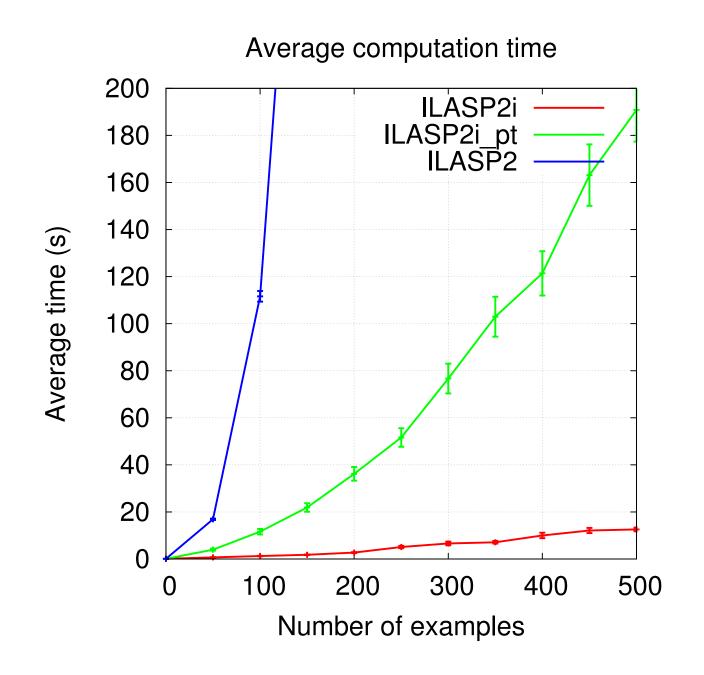
To scale up the number of counter-examples, context-dependent counter-examples can be considered.

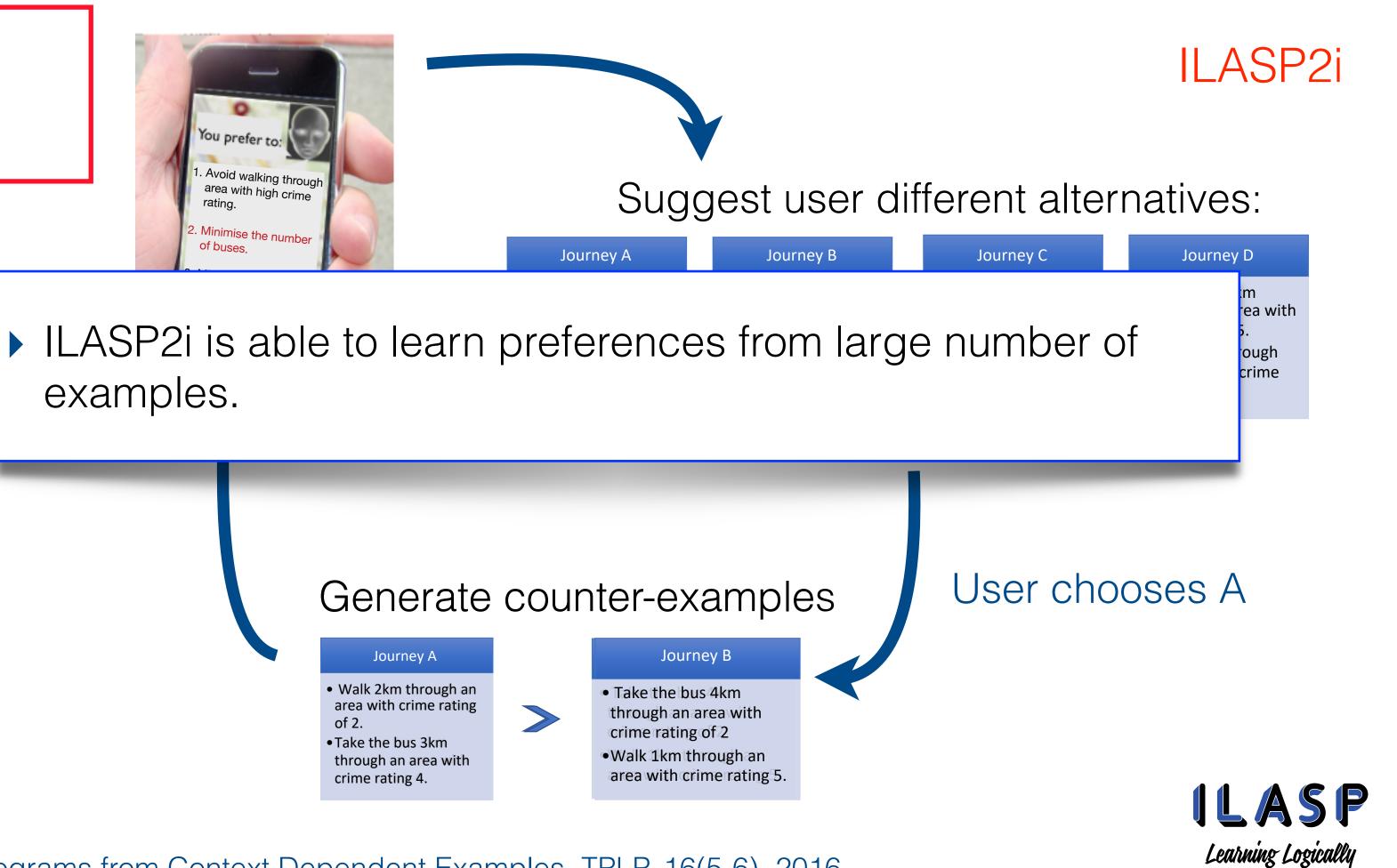




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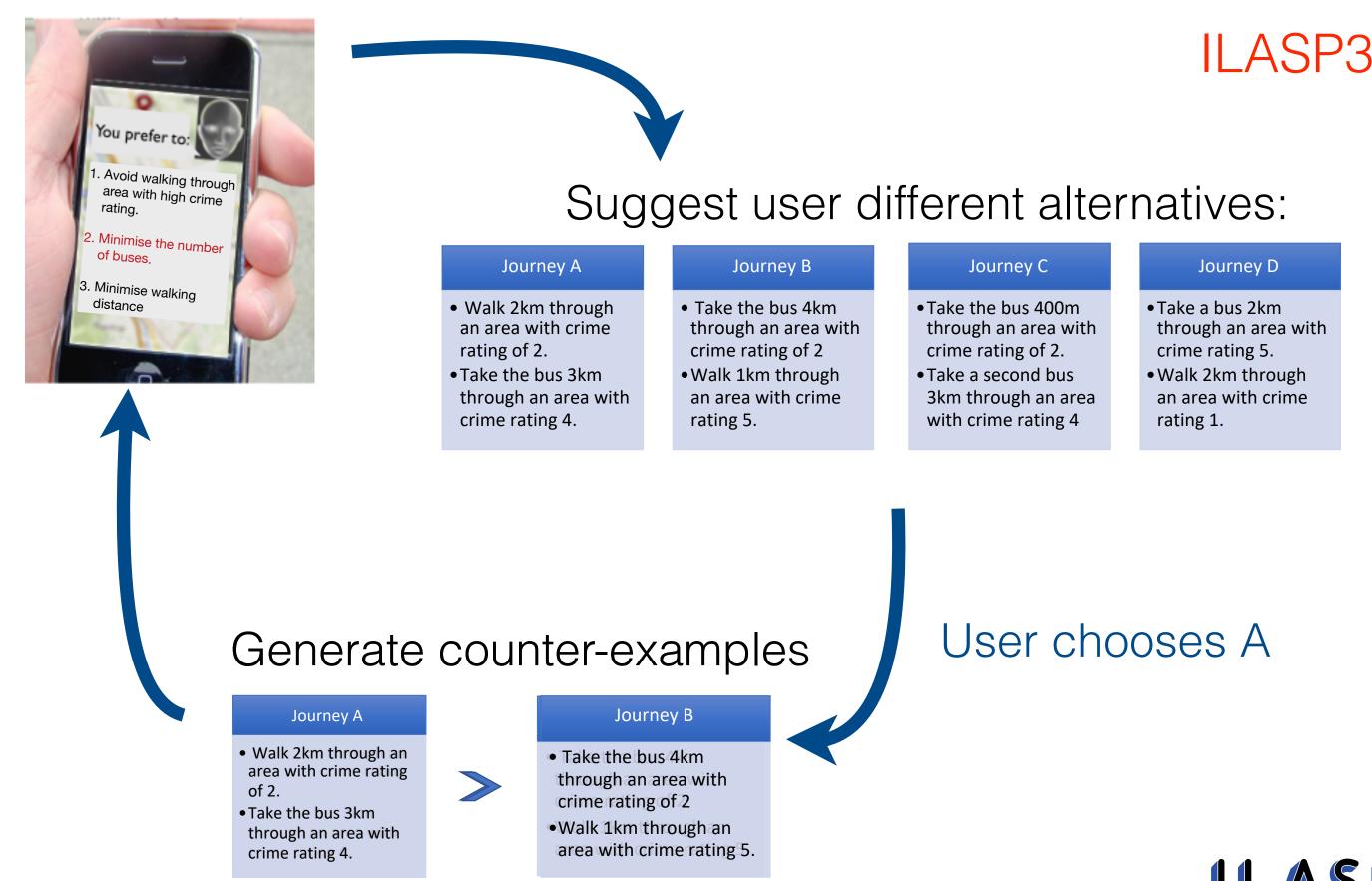
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Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Counter-examples might be noisy as humans might not know what they prefer.



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Counter-examples might be noisy as humans might not know what they prefer.

mislabelled

if it is not raining

if it is raining

Journey A

- Walk 2km through an area with crime rating
- Take the bus 3km through an area with crime rating 4.

Journey B

- Take the bus 4km through an area with crime rating of 2
- •Walk 1km through an area with crime rating 5.

• Walk 2km through an area with crime rating

Journey A

• Take the bus 3km through an area with crime rating 4.

Journey B

- Take the bus 4km through an area with crime rating of 2
- •Walk 1km through an area with crime rating 5.

. Avoid walking through area with high crime 2. Minimise the number of buses. 3. Minimise walking distance



Suggest user different alternatives:

 Walk 2km through an area with crime rating of 2.

Journey A

• Take the bus 3km through an area with crime rating 4.

Journey B

- Take the bus 4km through an area with crime rating of 2
- Walk 1km through an area with crime rating 5.

Journey C

- Take the bus 400m through an area with crime rating of 2.
- Take a second bus 3km through an area with crime rating 4

Journey D

ILASP3

- Take a bus 2km through an area with crime rating 5.
- Walk 2km through an area with crime rating 1.

User chooses A

Journey A

- Walk 2km through an area with crime rating of 2.
- Take the bus 3km through an area with crime rating 4.



Generate counter-examples

• Take the bus 4km through an area with crime rating of 2

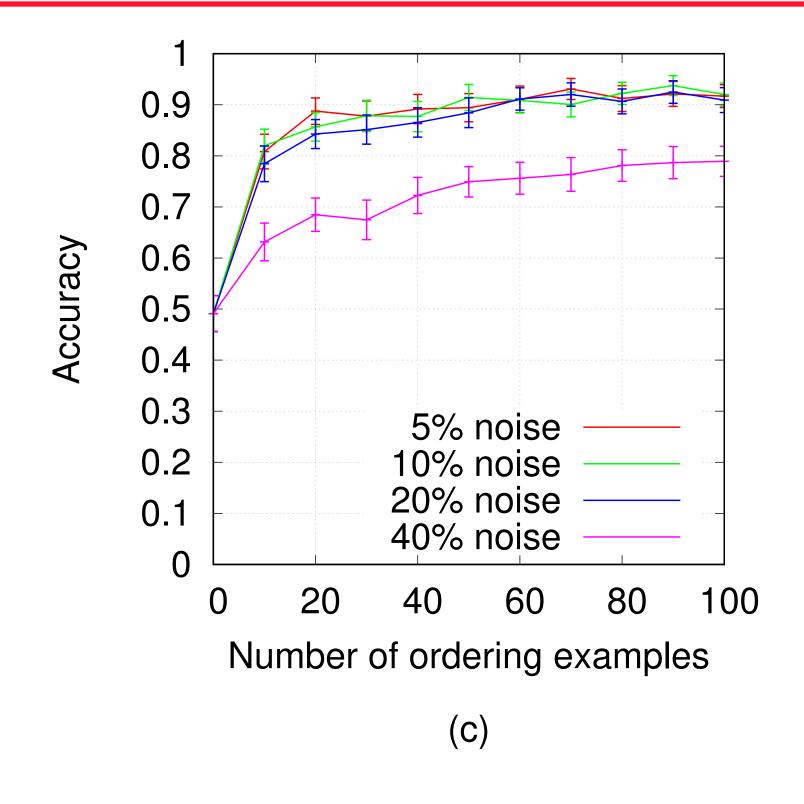
Journey B

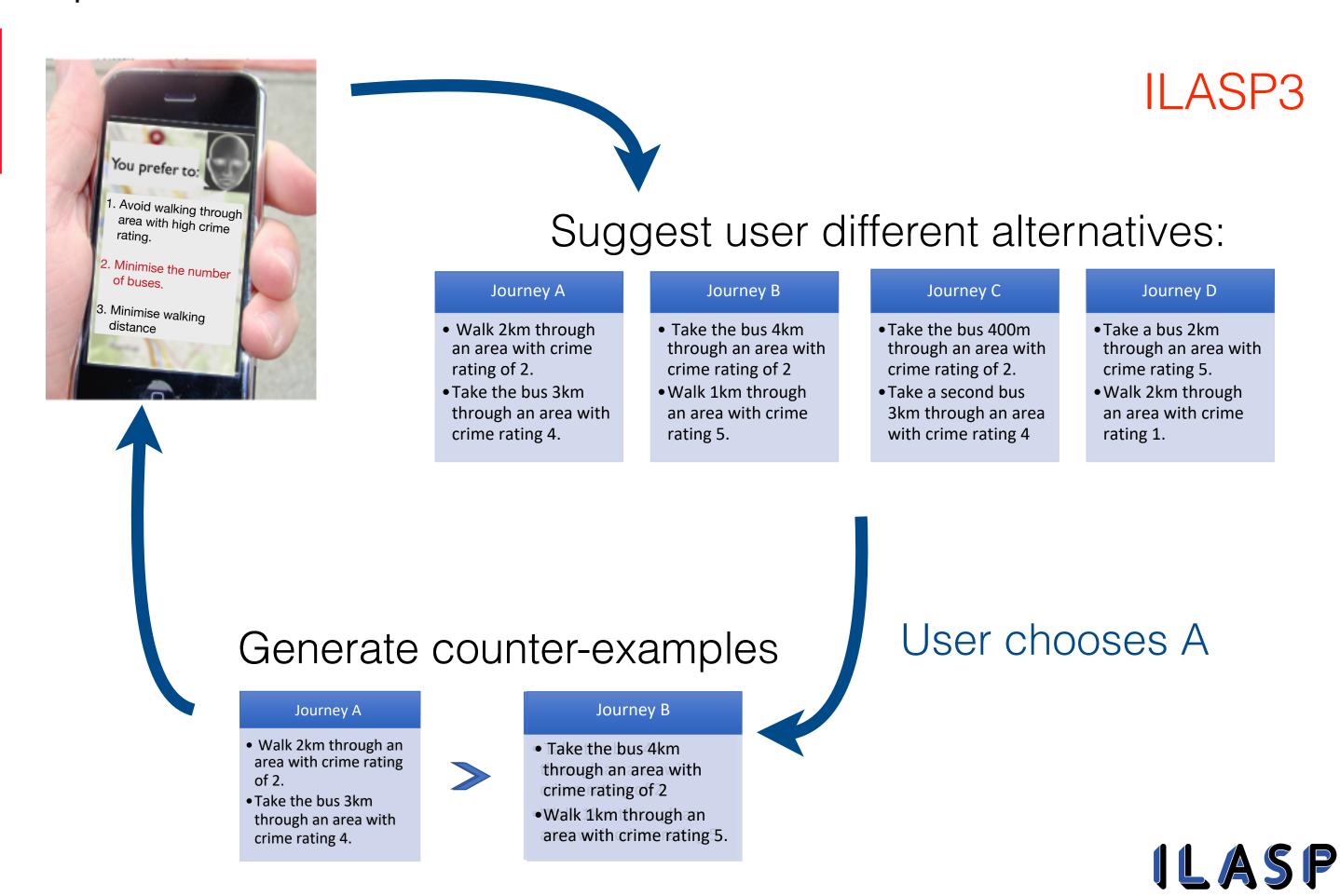
 Walk 1km through an area with crime rating 5.



Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Counter-examples might be noisy as humans might not know what they prefer.

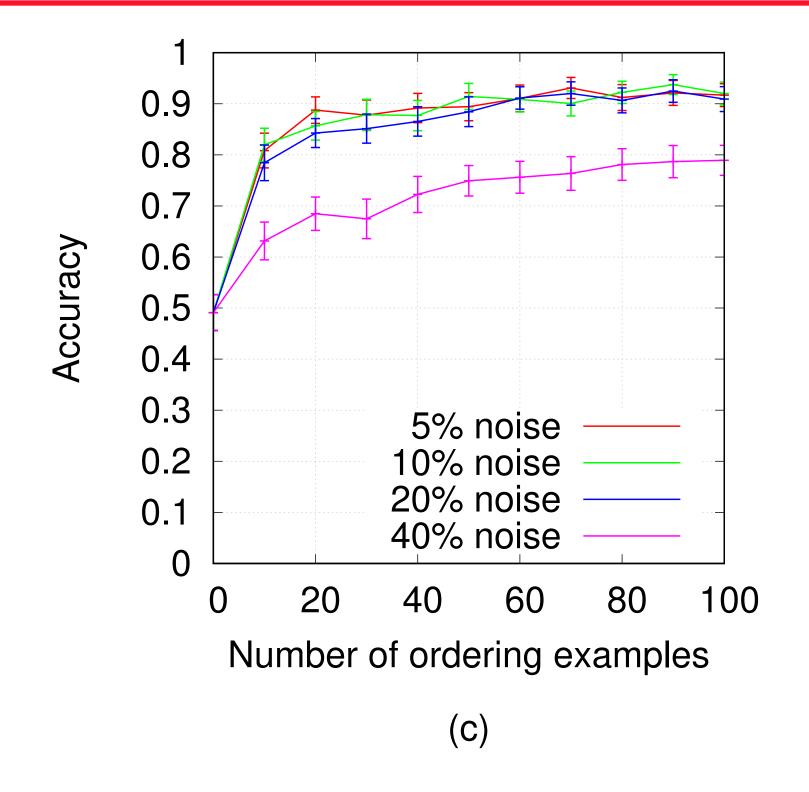


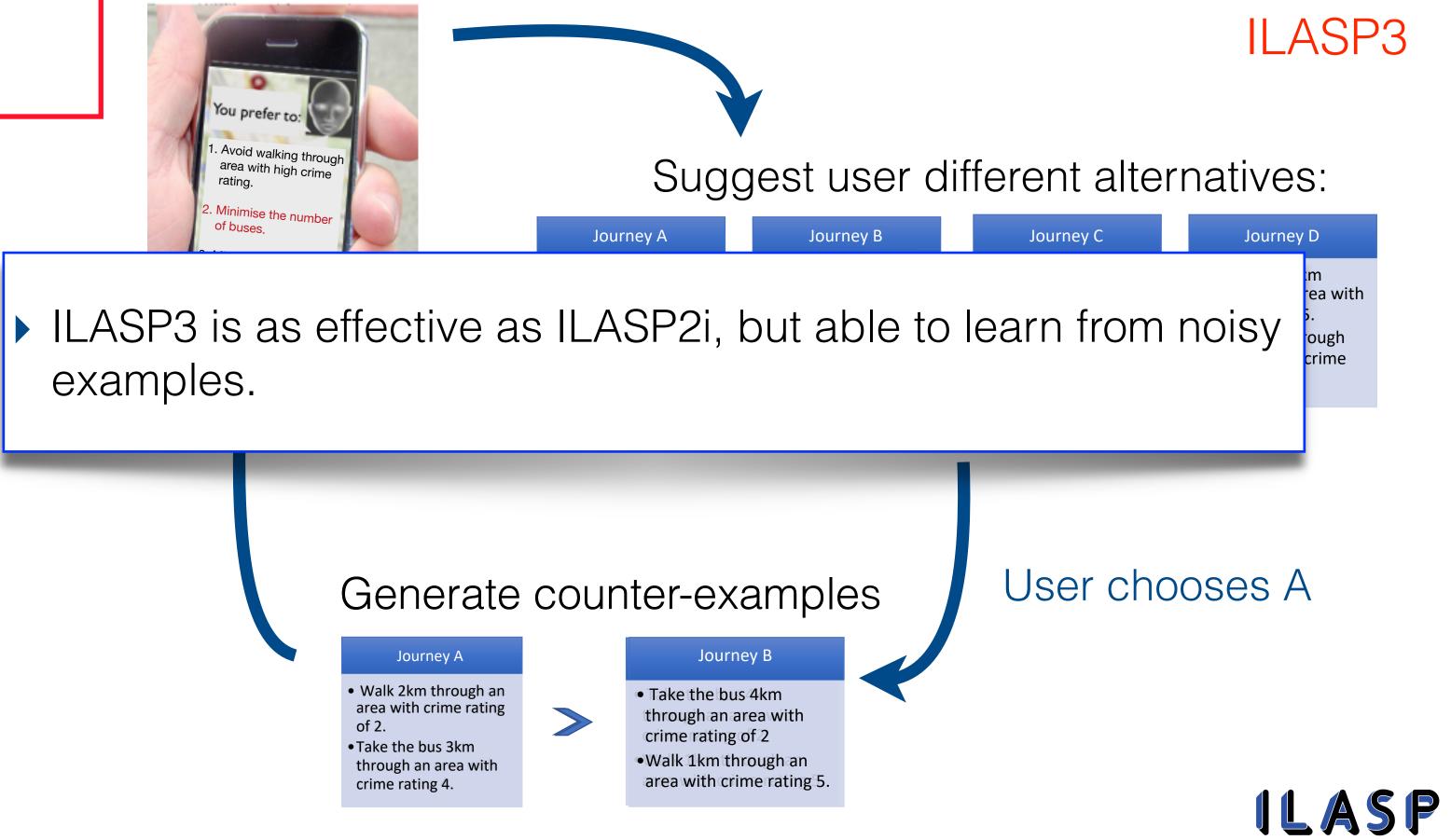


Learning Logically

Objective is to learn human preferences from human's choices, and provide them with optimal, personalised suggestions with explanation.

Counter-examples might be noisy as humans might not know what they prefer.





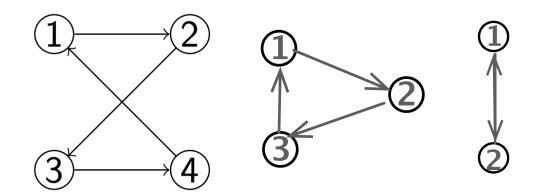
Learning Logically

Symbolic Machine Learning is highly declarative, and capable of learning definitions of complex (NP-hard) decision problems.

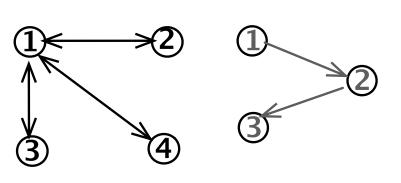
Background:

```
1{ size(1), size(2), size(3), size(4) } 1.
node(1..S) :- size(S).
0{ edge(V0, V1) } 1 :- node(V0), node(V1).
```

Positive examples:



Negative examples:

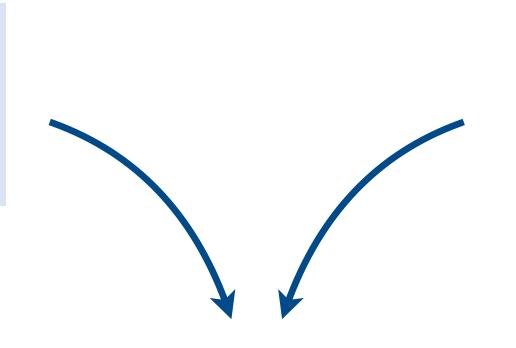




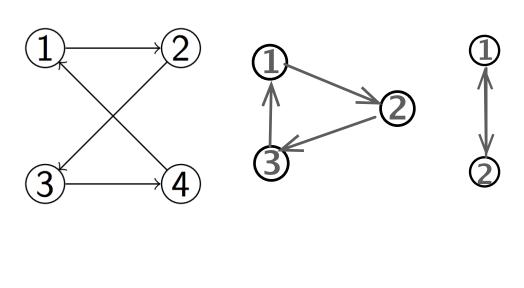
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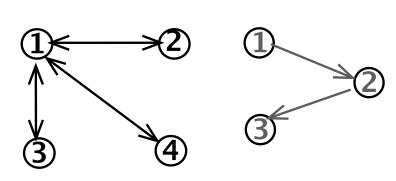
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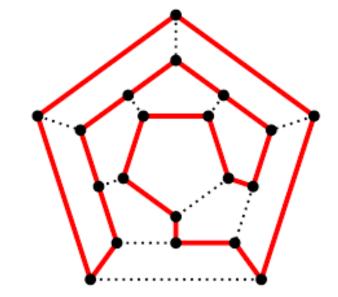


Positive examples:



Negative examples:





Learned definition of Hamiltonian graph:

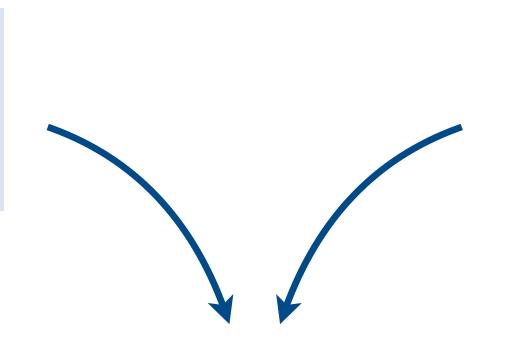
```
O{ in_hc(V0,V1) }1 :- edge(V0,V1)
reach(V0) :- in_hc(1,V0)
reach(V1) :- in_hc(V0,V1), reach(V0)
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:- in_hc(V0,V1), in_hc(V0,V2), V1≠ V2
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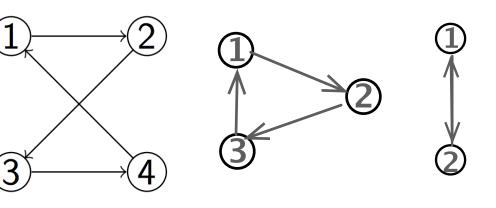
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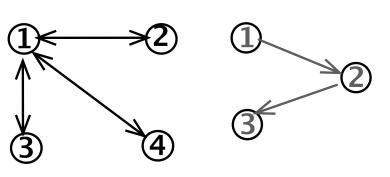
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Positive examples:



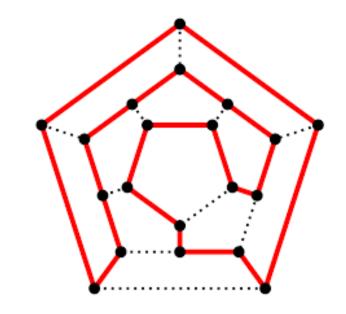
Negative examples:





```
O{ in_hc(V0,V1) }1 :- edge(V0,V1)
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A Hamilton cycle is a subset of the edges in the graph.

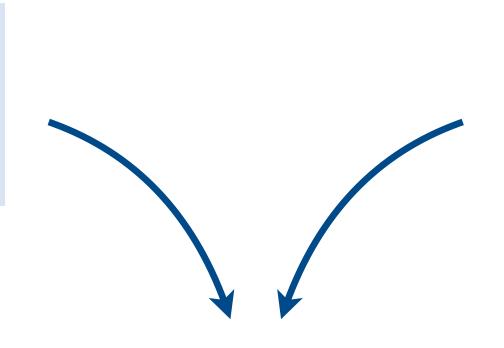




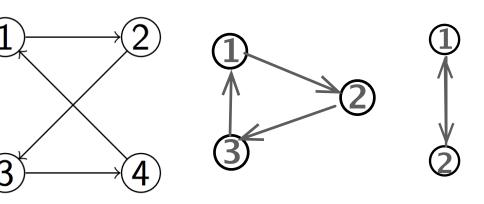
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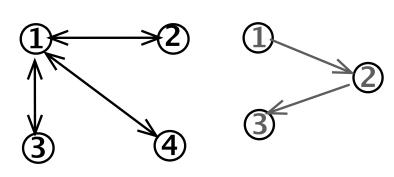
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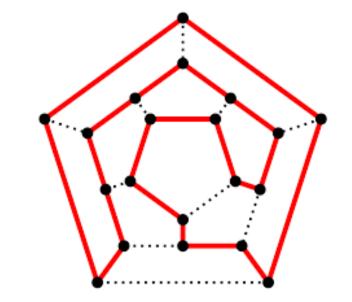


Node *n* is "reachable" if there is a path from node 1 to *n*.

Learned definition of Hamiltonian graph:

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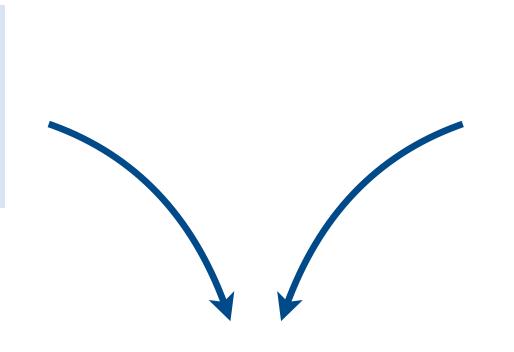




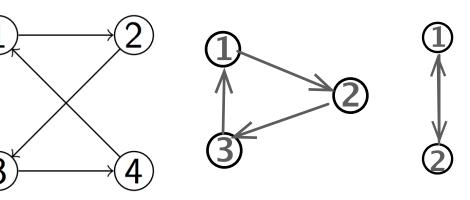
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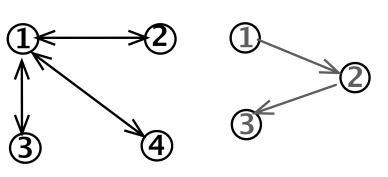
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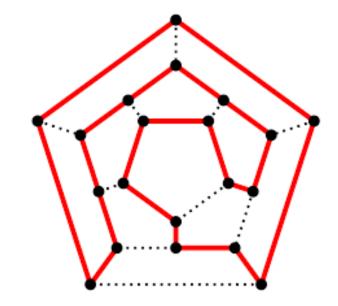
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A Hamilton cycle is a subset of the edges in the graph.

Every node must be reachable.

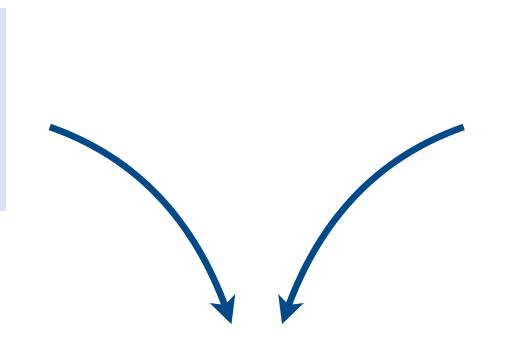




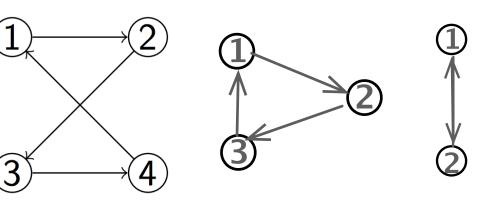
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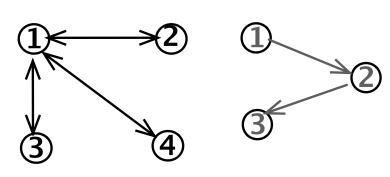
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```



Positive examples:



Negative examples:



Node *n* is "reachable" if there is a path from node 1 to *n*.

No node has more than one outgoing edge in the cycle.

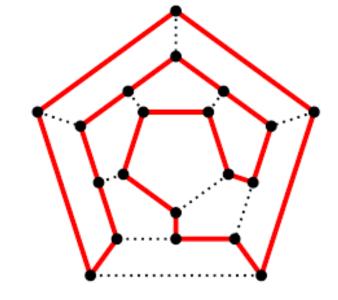
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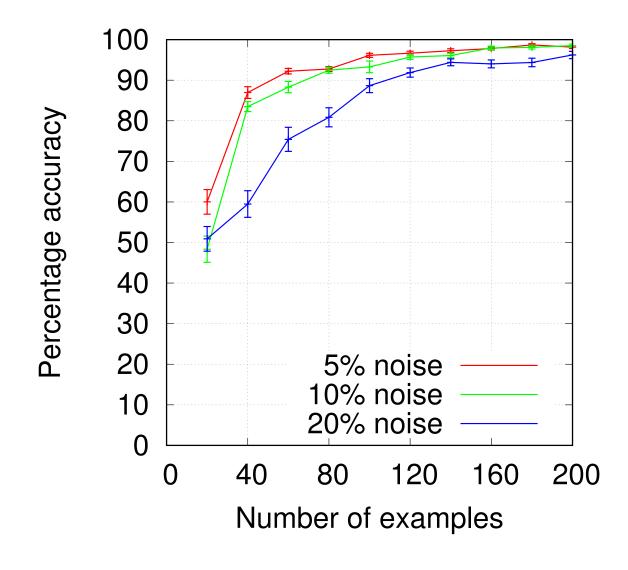
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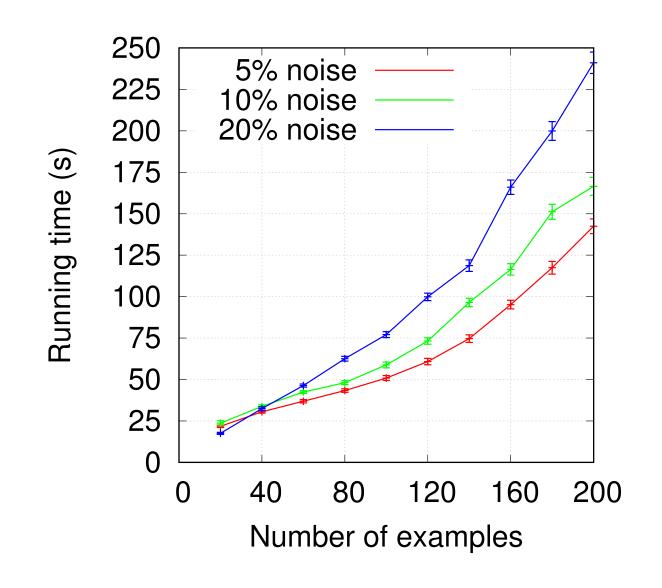




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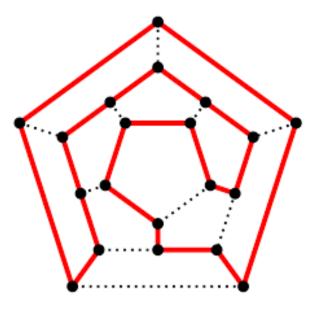
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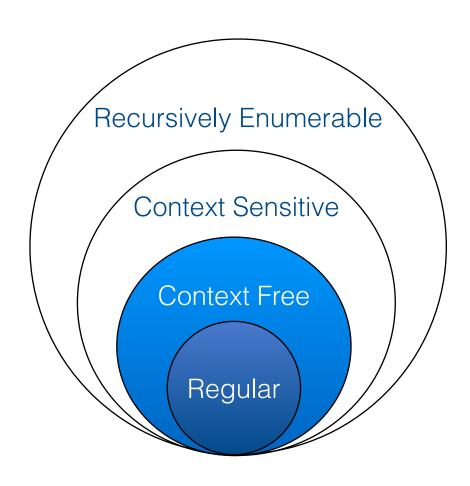
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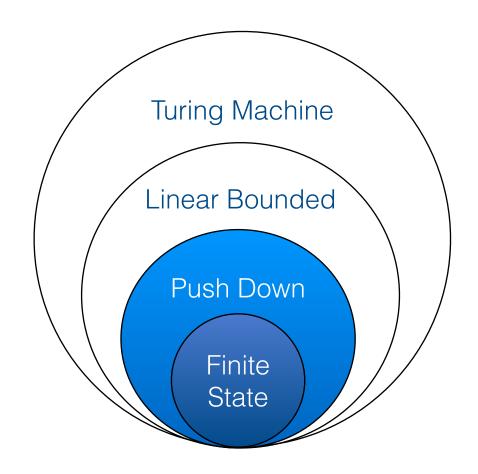
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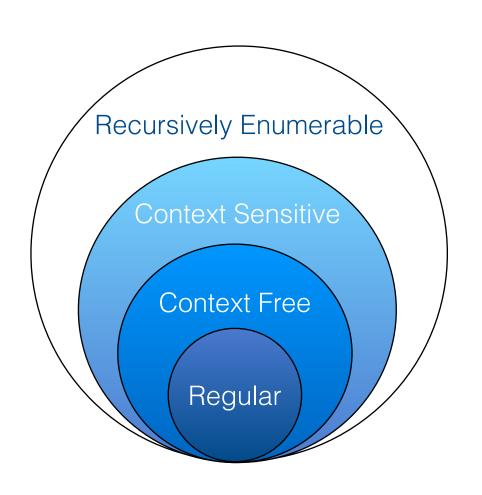
Previous work on learning grammars and automata has mostly been restricted to Regular Grammars (FSA) and Context-free Grammars (PDA).

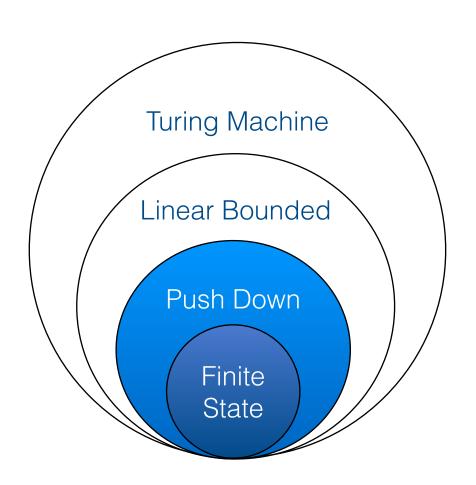






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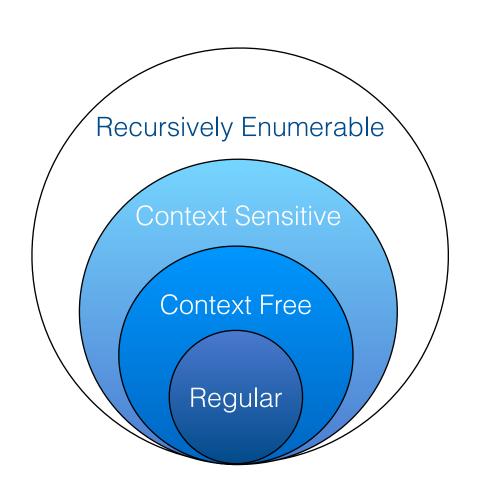


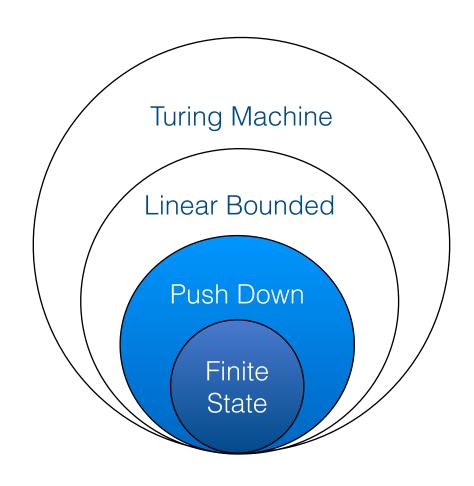
Learn a class of context-sensitive grammars (ASG):

- context-free part defines the syntax of the language
- context-sensitive parts defines semantics.



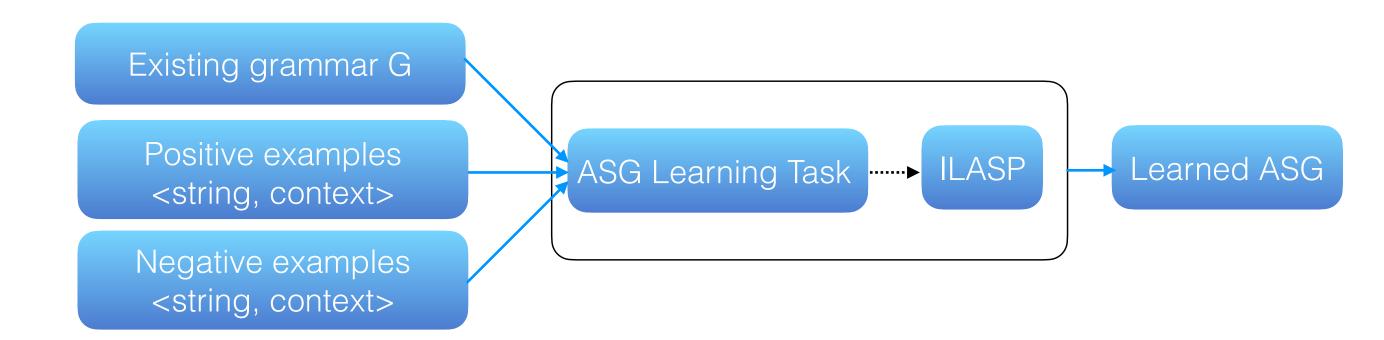
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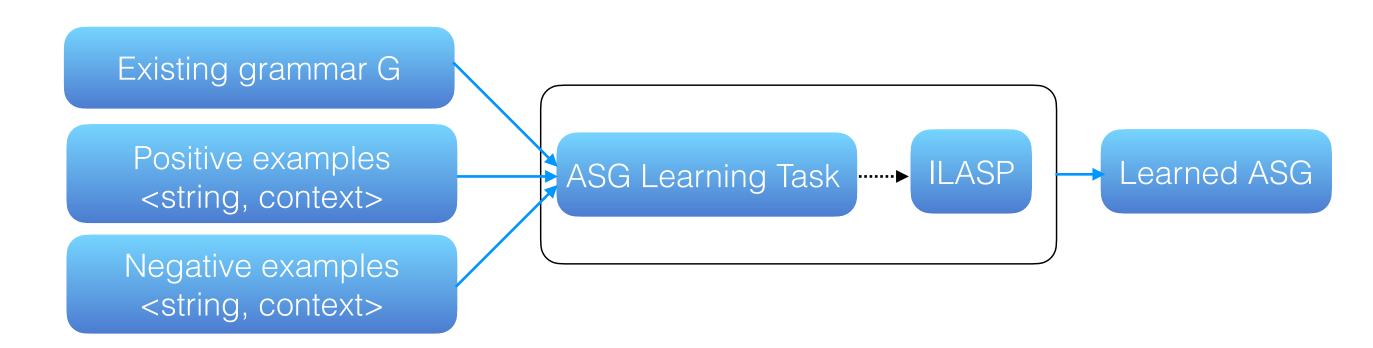




Example of context-sensitive grammar

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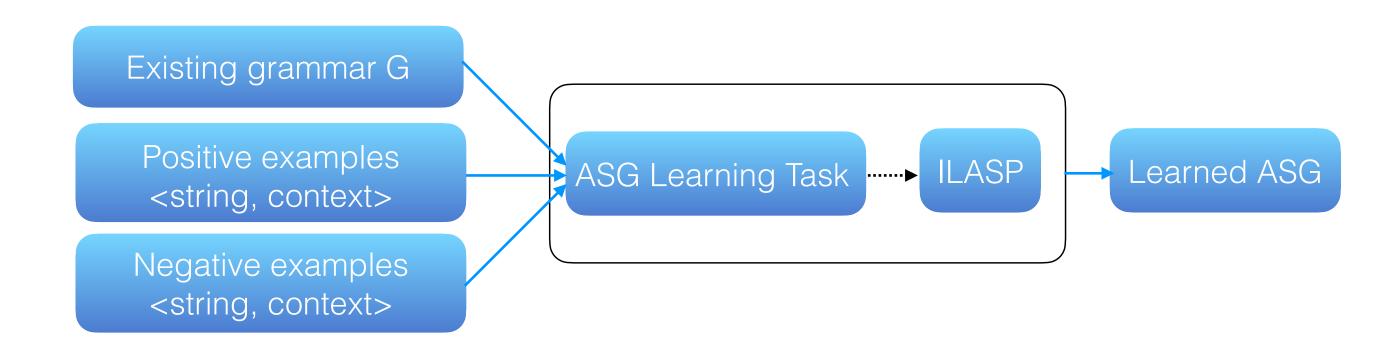


Example of context-sensitive grammar

```
start -> as bs cs { false \leftarrow size(X)@1, not size(X)@2 false \leftarrow size(X)@1, not size(X)@2 } as -> "a" as { size(X+1) \leftarrow size(X)@2 } as -> "b" bs { size(0) } bs -> "b" bs { size(0) } cs -> "c" cs { size(X+1) \leftarrow size(X)@2 } cs -> "c" cs { size(X+1) \leftarrow size(X)@2 } cs -> "size(0) }
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```

√"abc"

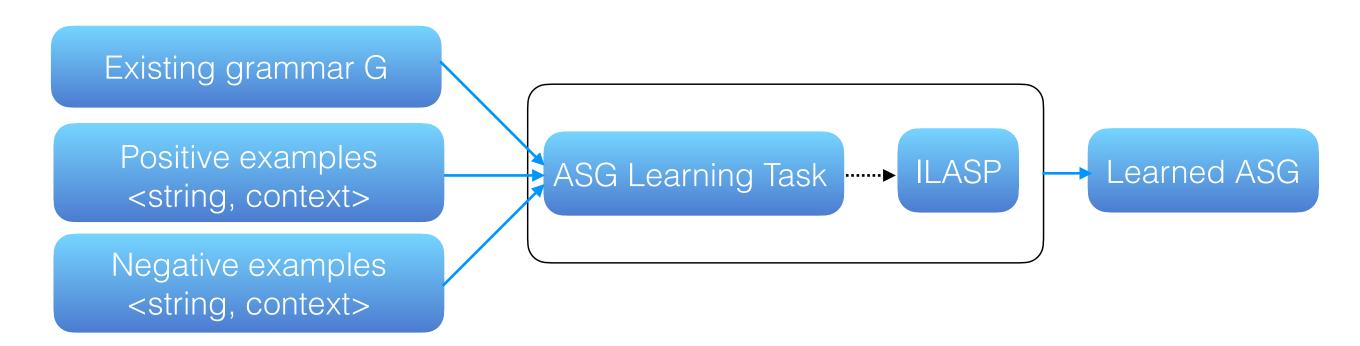
√"anbncn"

x "ac"

is accepted by $\mathcal{L}(G)$ is accepted by $\mathcal{L}(G)$ is not accepted by $\mathcal{L}(G)$

Learn a class of context-sensitive grammars (ASG):

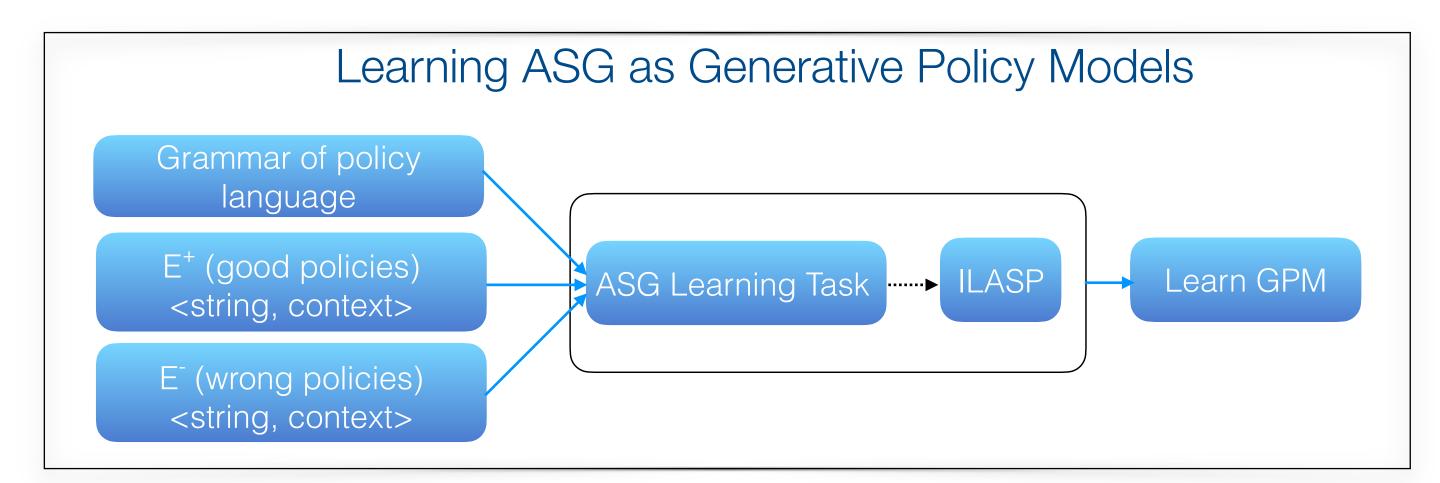
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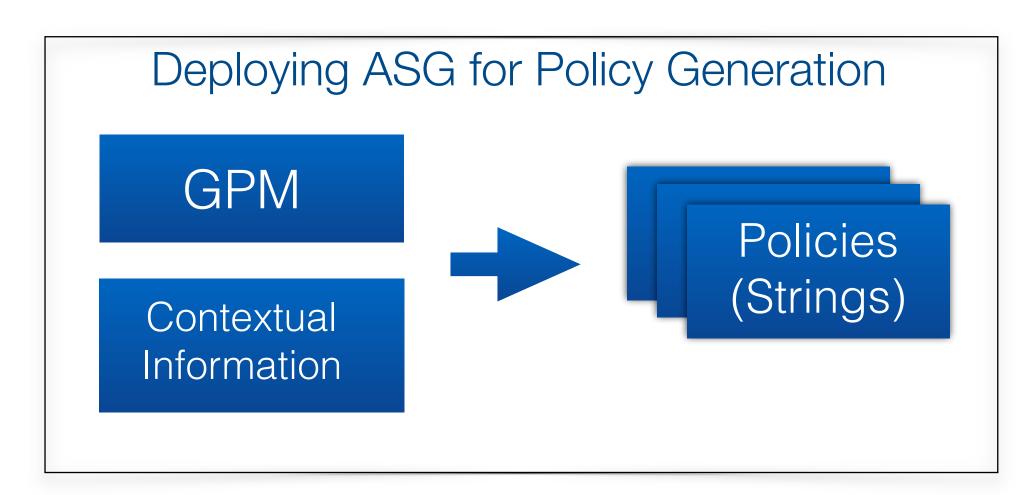




Learning Generative Policy Models

- Intelligent devices/systems need to self-configure to adapt their behaviour in dynamic and complex contexts.
- Generative Policy Model (GPM): a solution for automatic, context-aware generation of policies





Applications

- Autonomous vehicle scenario
- Learning access control policies
- Logistic resupply scenario



Summary of SOTA of Symbolic Learners

System	Normal Rules	Constraints	Non- determinism	Preferences	Context	Noise	Optimal
ASPAL	✓	X	X	X	X	X	√
XHAIL	√	X	X	X	X	✓	X
ILED	✓	X	X	X	X	X	X
OLED	✓	X	X	X	X	✓	X
Inspire	✓	X	X	X	X	✓	X
ILASP	✓	✓	✓	✓	✓	✓	✓

Summary of SOTA of Symbolic Learners

System	Normal Rules	Constraints	Non- determinism	Preferences	Context	Noise	Optimal
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Two Misconceptions Resolved:

- Complex models expressing recursive concepts, non-monotonic assumptions, constraints, preferences, <u>can be</u> efficiently learned by ILASP.
- ▶ ILASP <u>is robust to noise</u> in the data.

Summary of SOTA of Symbolic Learners

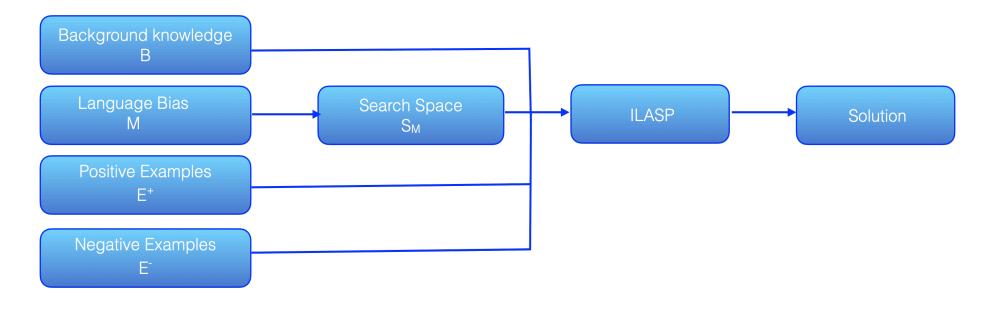
System	Normal Rules	Constraints	Non- determinism	Preferences	Context	Noise	Optimal
ASPAL	✓	×	×	X	×	×	✓
XHAIL	✓	×	X	X	×	✓	X
ILED	✓	×	×	X	×	X	X
OLED	✓	X	X	X	X	✓	X
Inspire	✓	X	X	X	X	✓	X
ILASP	√	✓	✓	✓	✓	√	√

Two Misconceptions Resolved:

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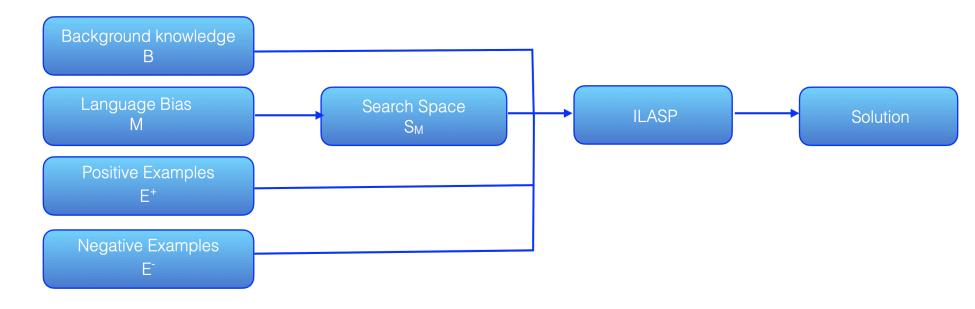
What about scalability?

ILASP

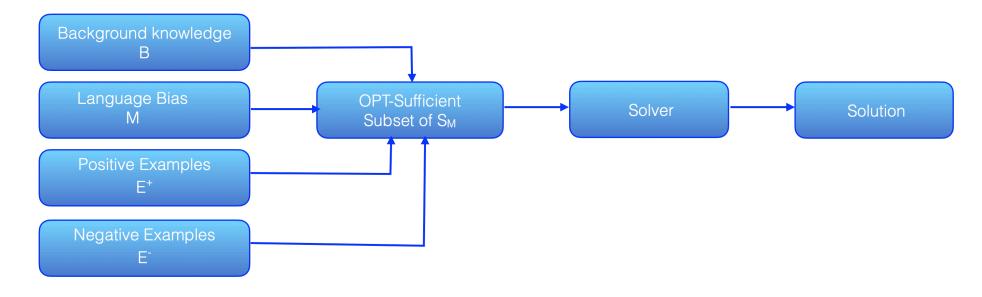




ILASP

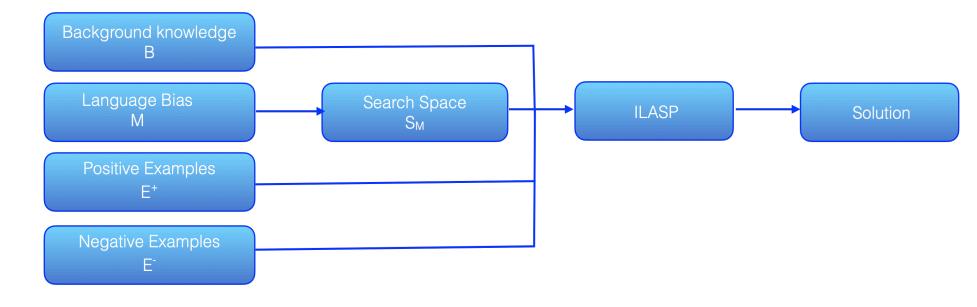


FastLAS

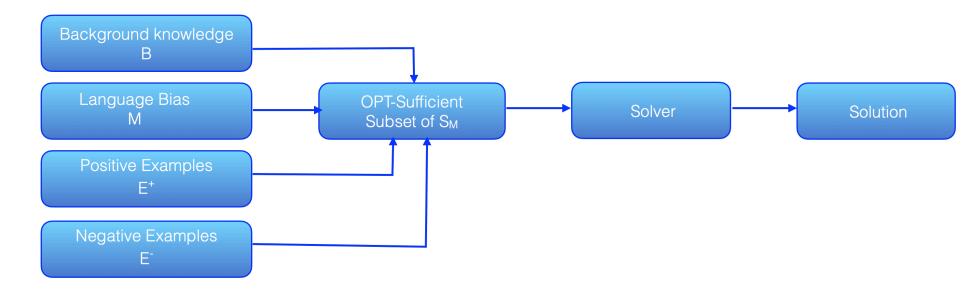




ILASP



FastLAS



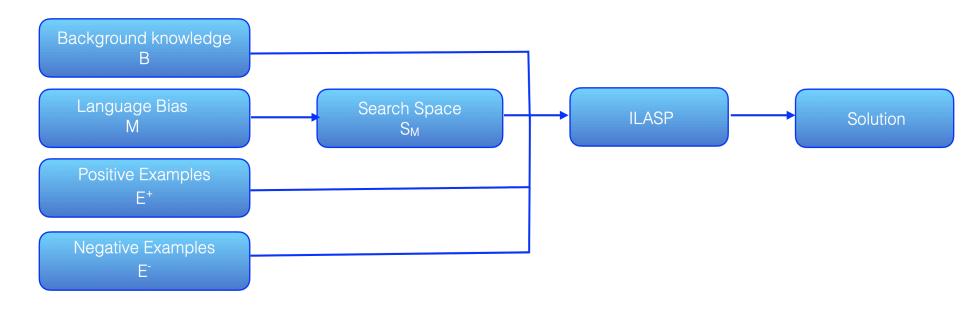
Event detection - CAVIAR dataset



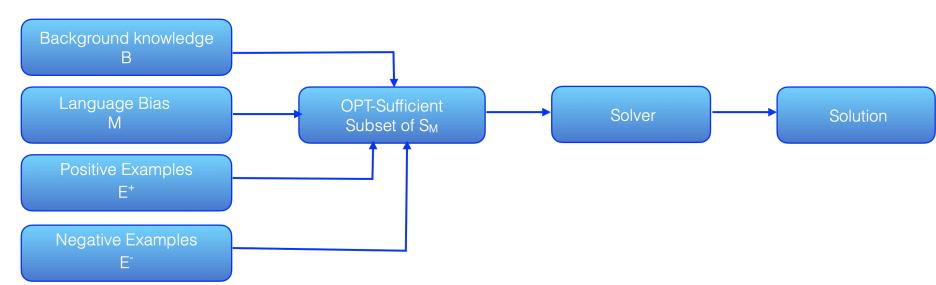
Learn a model that detects people meeting



ILASP



FastLAS



Event detection - CAVIAR dataset



Learn a model that detects people meeting

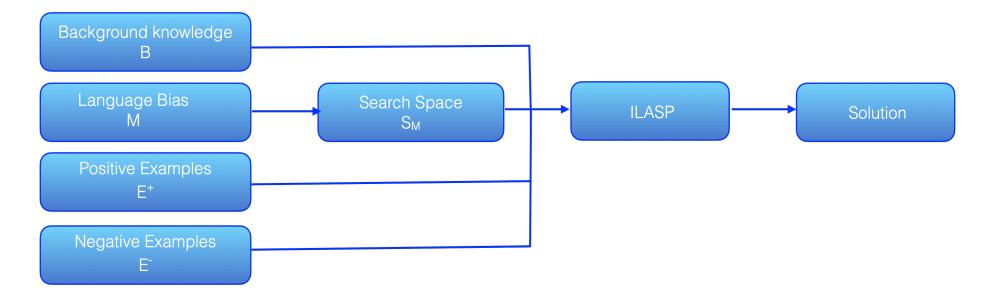
System	F_1	Running Time
OLED	0.792	107s
ILASP3	0.837	523.3s
FastLAS	0.907	263.8s

 $S_M = 3370 \text{ rules}$

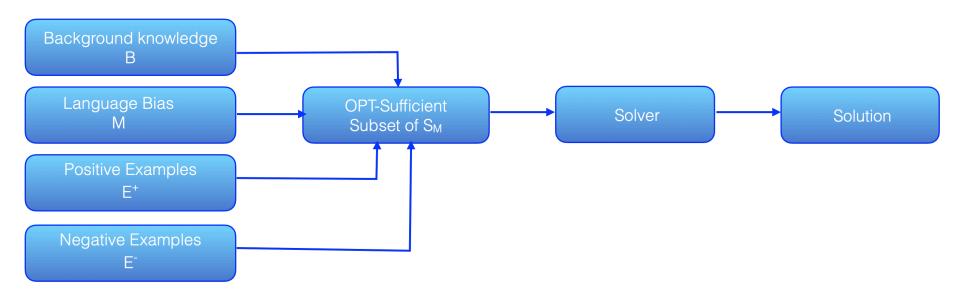
 $S_M = 2^{44} \text{ rules}$



ILASP



FastLAS



Event detection - CAVIAR dataset



Low-level features (e.g. people's location) already extracted

Learn a model that detects people meeting

System	$ F_1 $	Running Time
OLED	0.792	107s
ILASP3	0.837	523.3s
FastLAS	0.907	263.8s

 $S_M = 3370 \text{ rules}$

 $S_M = 2^{44} \text{ rules}$

What about if data are unstructured?



Facebook's bAbl dataset

Story:

- I. John went to the local restaurant.
- 2. The waiter brought John a glass of water and took the order.
- 3. As John was waiting, he took out the book and began to read it.
- 4. The steak which he ordered finally arrived.
- 5. After John had finished the meal, he took the jacket but he forgot to take the book.
- 6. He paid the bill and went back to the hotel.

Questions:

- I. Where is John?
- 2. Where was John before he went to the hotel?
- 3. Who took the order?
- 4. Who received a glass of water?
- 5. Did John have to wait?
- 6. What did John read?
- 7. What did John choose?
- 8. Where is the book?
- 9. Where is the jacket?

Facebook's bAbl dataset

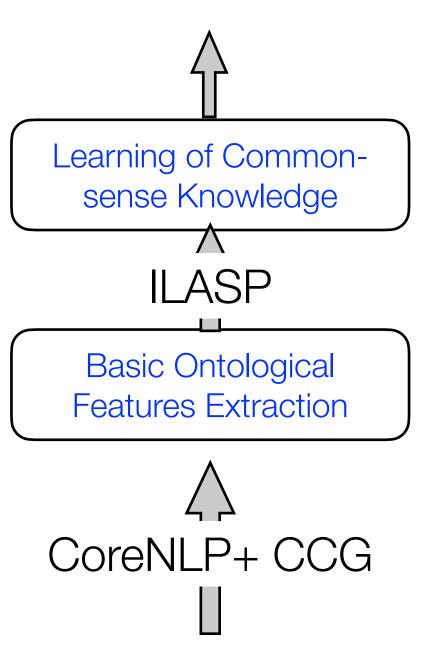
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CorrectAnswer



text, question and answers (correct and incorrect)

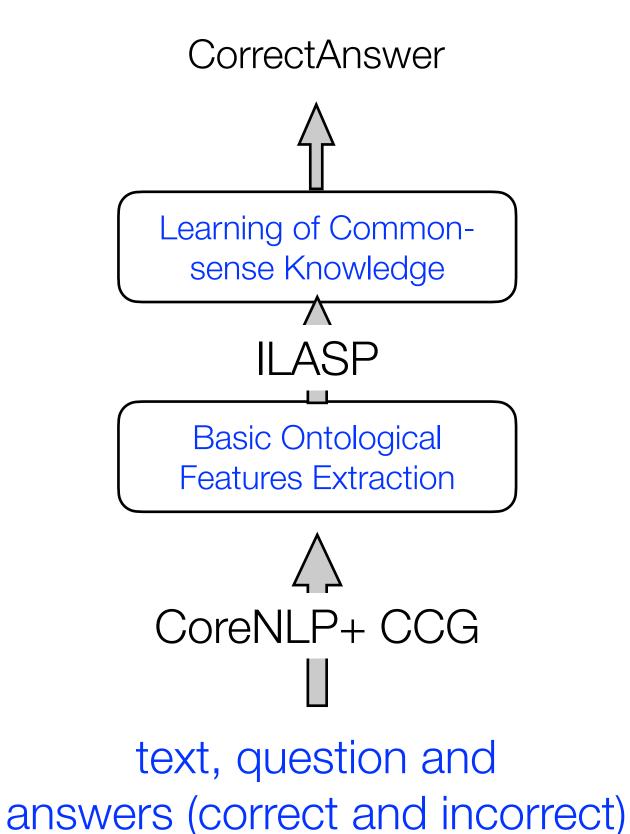
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Automated semantic representation of English text into logic-based knowledge.

Facebook's bAbl dataset

Story:

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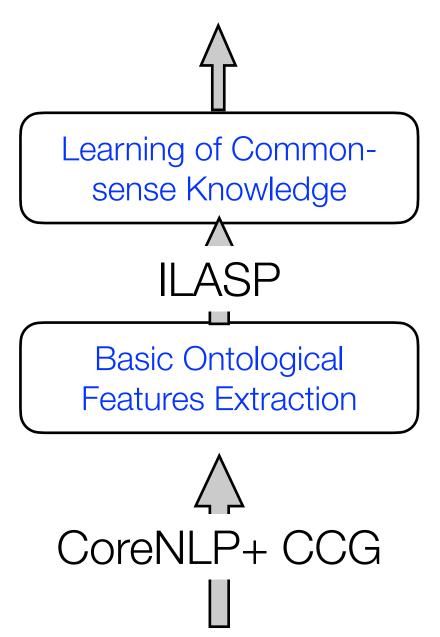
Questions:

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- 3. Who
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 8. Wheten
- 9. Whe

	Task										
Ex.	1	6	8	9	12	15	18				
5	64.8	90.7	92.4	74.6	100.0	100.0	81.7				
10	100.0	90.7	92.4	81.8	100.0	100.0	87.9				
15	100.0	92.0	100.0	90.6	100.0	100.0	91.2				
20	100.0	95.8	100.0	94.6	100.0	100.0	88.2				
25	100.0	98.9	100.0	97.0	100.0	100.0	92.4				

	Task							
System	1	6	8	9	12	15	18	
Sukhbaatar et al. (MemN2N)	99.9	98.0	93.9	98.5	100.0	98.2	90.8	
Henaff et al. (EntNet)	99.3	70.0	80.8	68.5	99.2	42.2	91.2	
Report $(CCG + ILASP)$	100.0	98.9	100.0	97.0	100.0	100.0	92.4	

CorrectAnswer



text, question and answers (correct and incorrect)

Automated semantic representation of English text into logic-based knowledge.

FastLAS

- ✓ Orders of magnitude faster that state-of-the-art ILASP
- ✓ Can solve machine learning tasks with much larger search spaces
- ✓ Sound and complete guaranteed to find an optimal solution

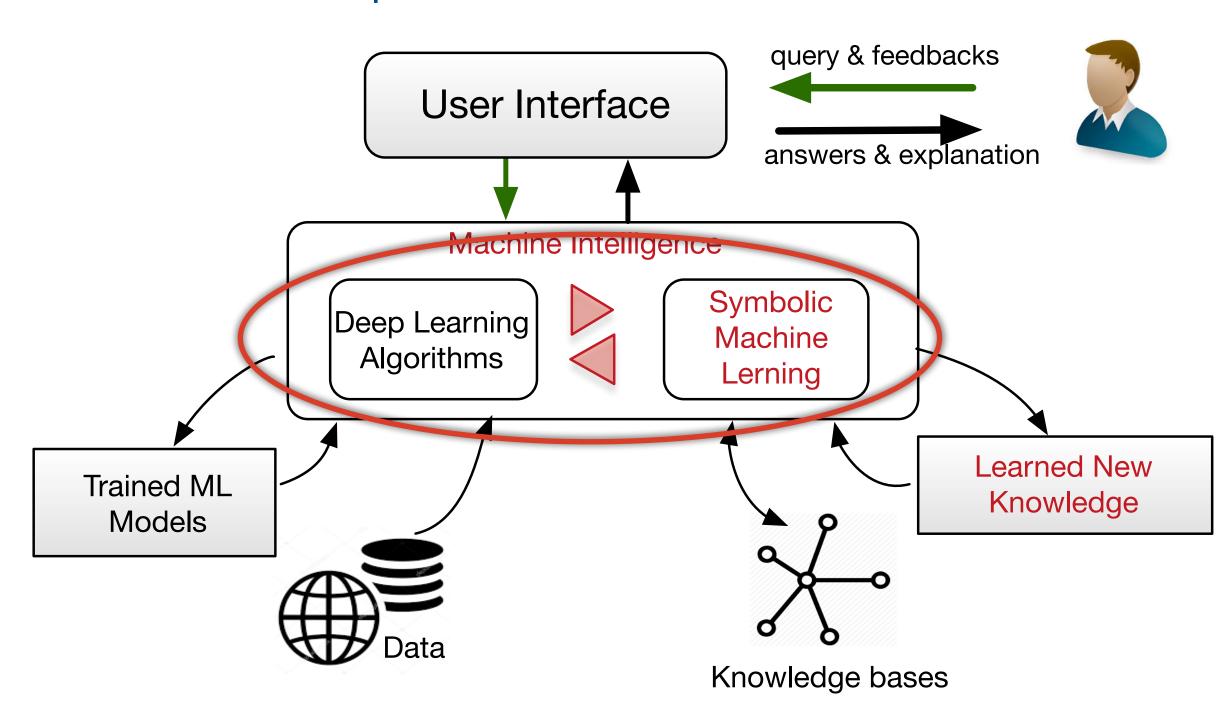
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- * Requires structured data

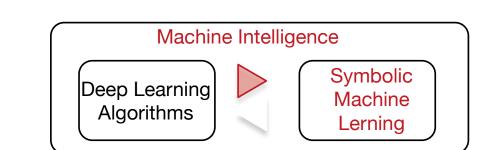
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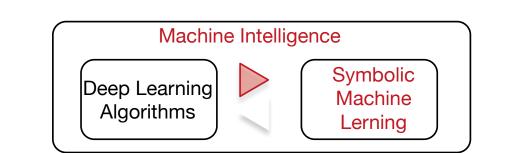
How effective is symbolic rule learning from labelled unstructured data, when contextual information is extracted by deep neural networks?



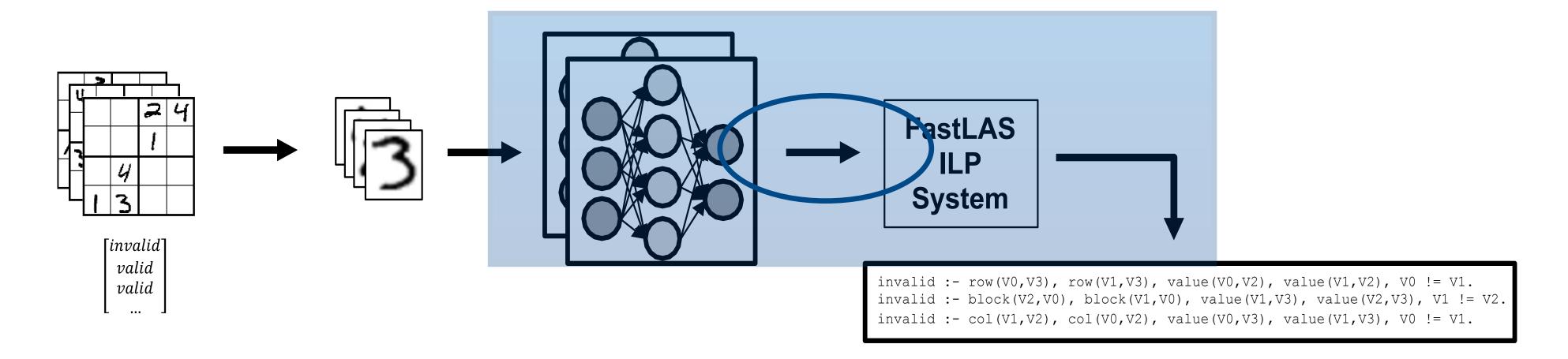
Hybrid Interpretable Learning from Noisy Raw Data



How effective is symbolic rule learning from labelled unstructured data, when contextual information is extracted by deep neural networks?

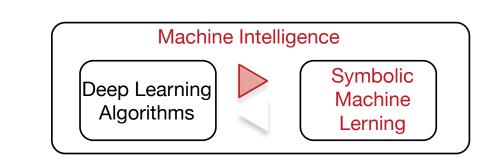


Hybrid Interpretable Learning from Noisy Raw Data





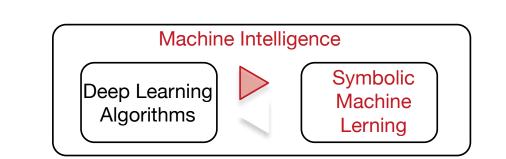
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Hybrid Interpretable Learning from Noisy Raw Data



How effective is symbolic rule learning from labelled unstructured data, when contextual information is extracted by deep neural networks?



Hybrid Interpretable Learning from Noisy Raw Data

Sudoku Board Classification

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Applied Perturbation to increasing % of training examples

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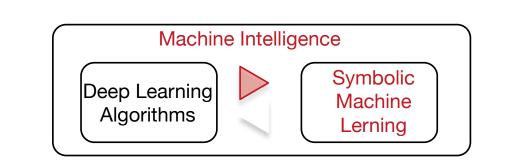
400 examples total

5-fold cross validation: Train split: 320 examples Test split: 80 examples

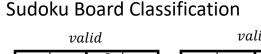




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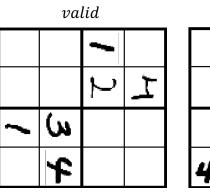
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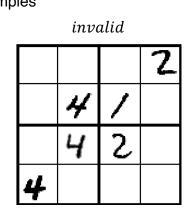


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Applied Perturbation to increasing % of training examples

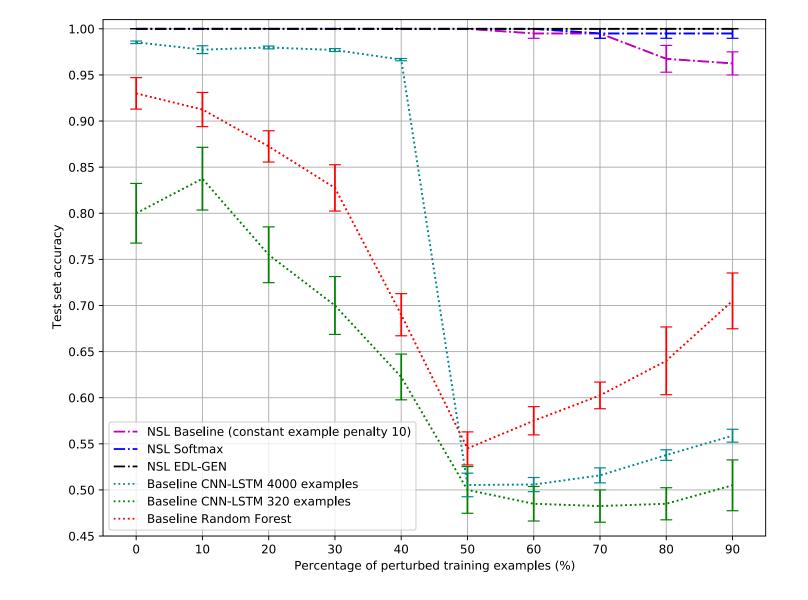
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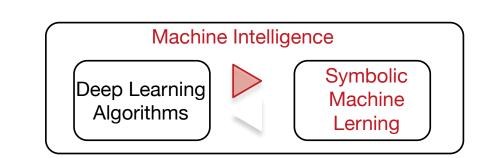
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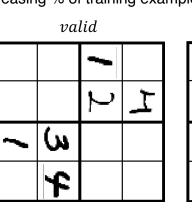
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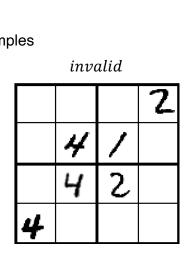
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valid					valid				invalid			
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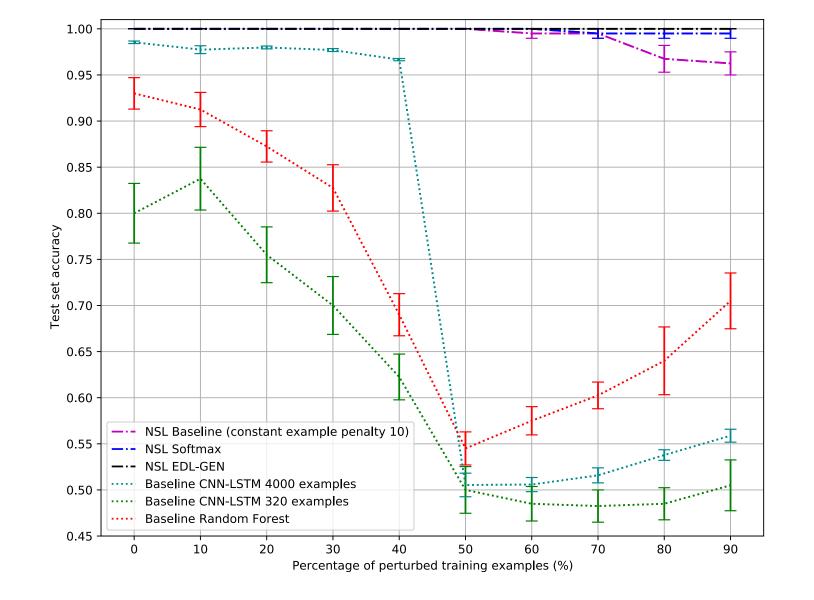
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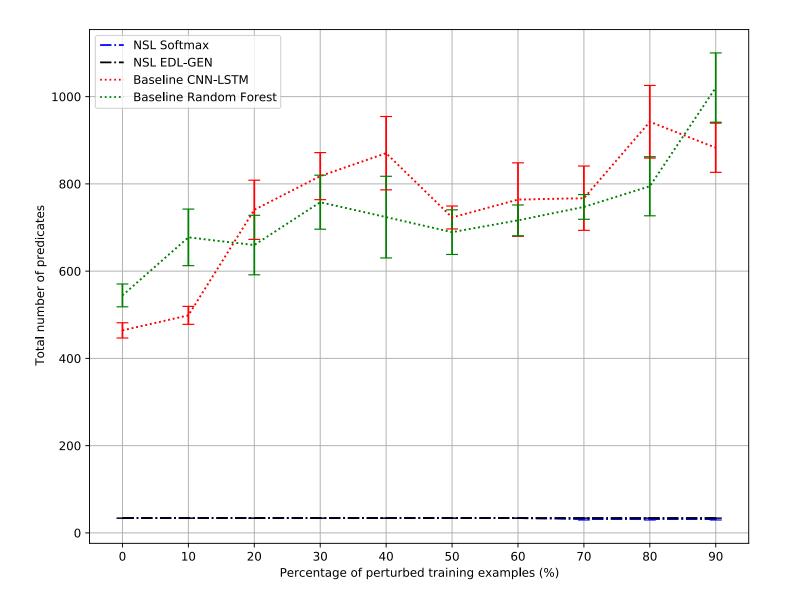




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In Summary

Symbolic Machine Learning is capable of

- Learning complex knowledge that expresses recursive concepts, non-monotonic conditions, constraints, preferences.
- Learning generalisations from noisy data without overfitting the data.
- Learning knowledge that is interpretable and that can be used to automatically generate explanations.
- Learning from unstructured data if integrated with sub-symbolic methods.

More needs to be done to:

- Handle uncertainty (if any) during the learning process and quantify the level of uncertainty of predictions.
- Realise an end-to-end neural-symbolic architecture.

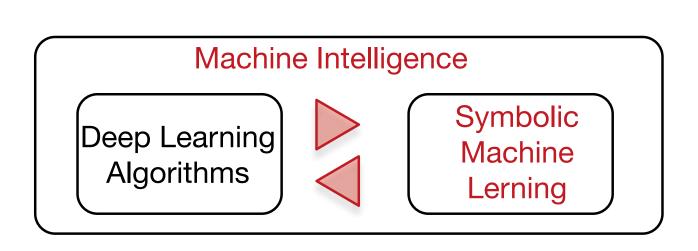
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Collaborators...







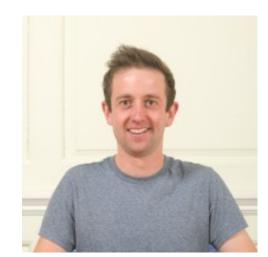
Domenico Corapi



Mark Law



Piotr Chabierski



Daniel Cunnington



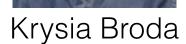
Jorge Lobo



Elisa Bertino

Collaborators...







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Jorge Lobo



Elisa Bertino

Thank you for listening!

Any questions 2

